

QuietOT: Lightweight Oblivious Transfer with a Public-Key Setup



Sacha Servan-Schreiber



Joint work with

Geoffroy Couteau, Lalita Devadas, Srinivas Devadas, and Alexander Koch

Secure Computation



Alice

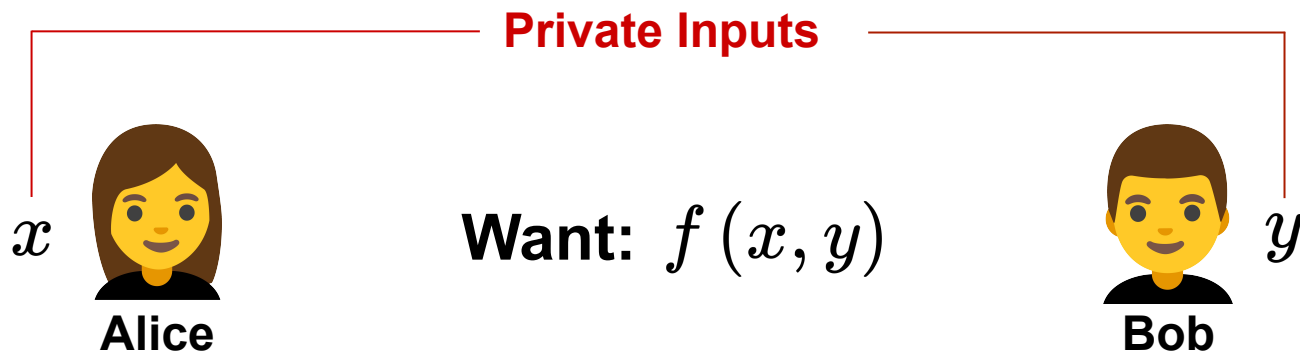


Bob

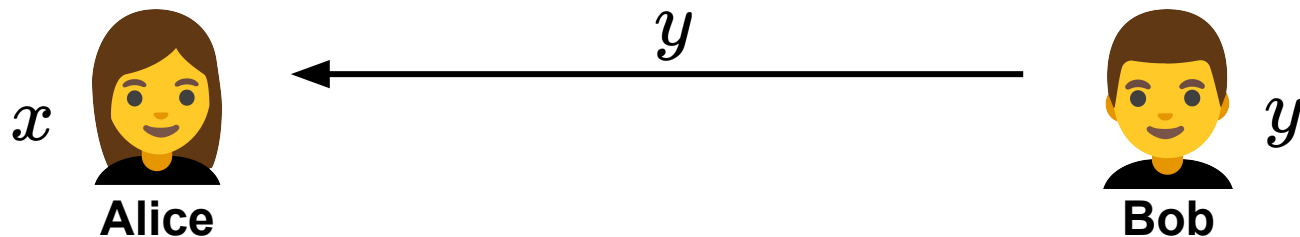
Secure Computation



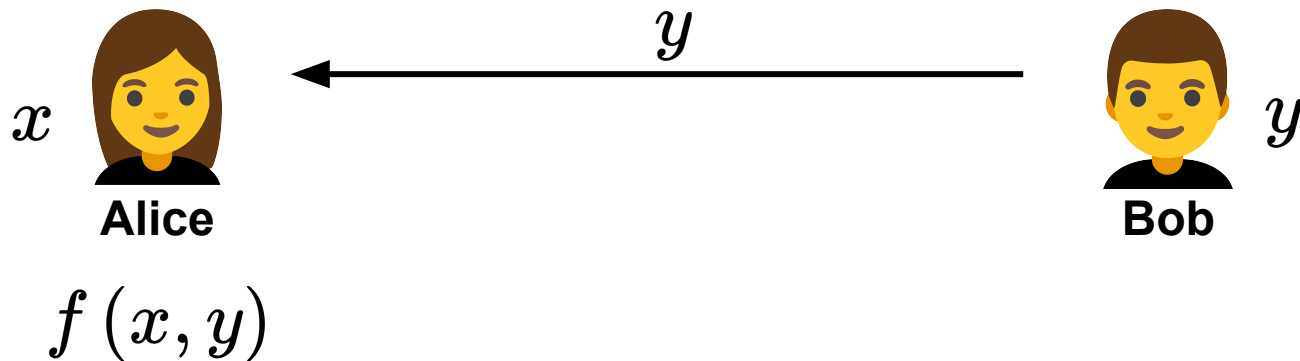
Secure Computation



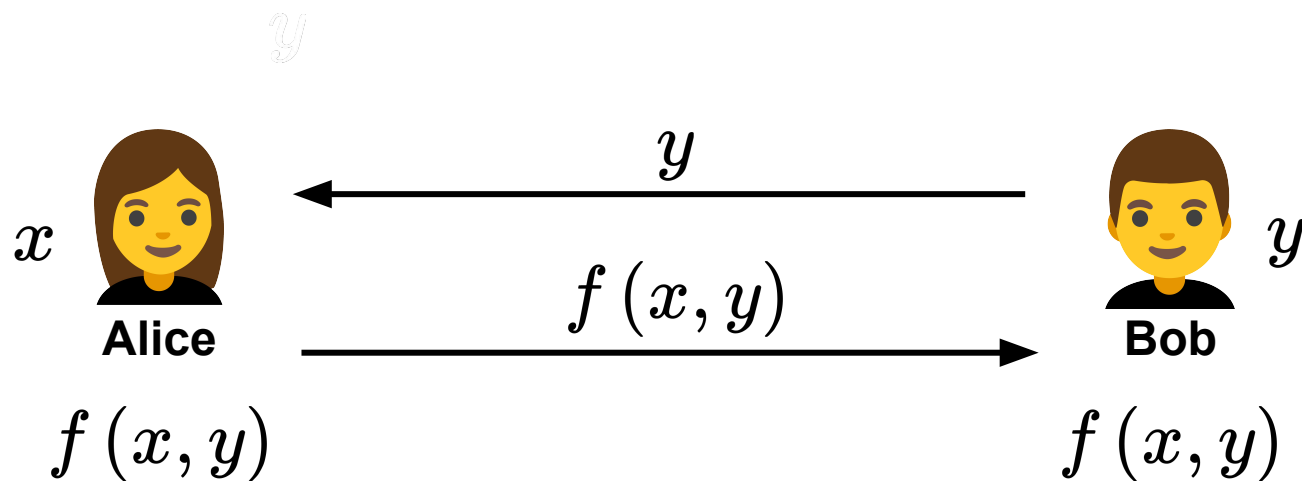
Secure Computation



Secure Computation

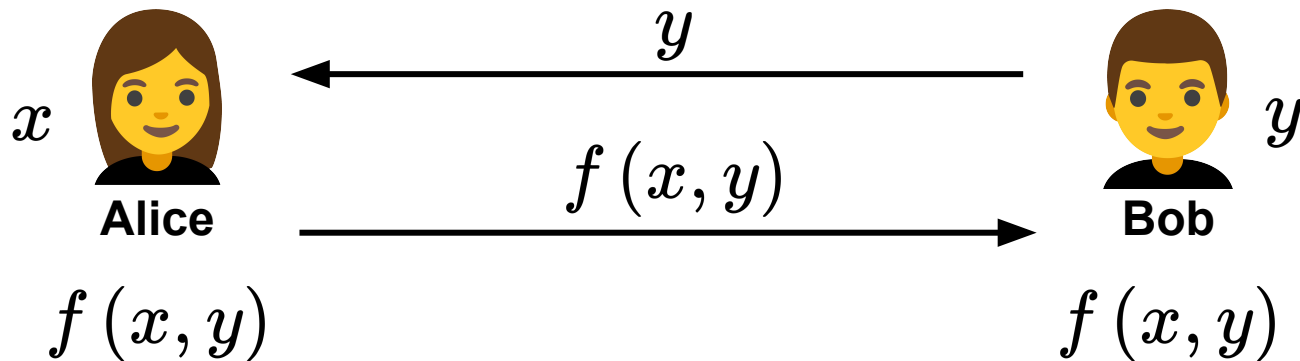


Secure Computation

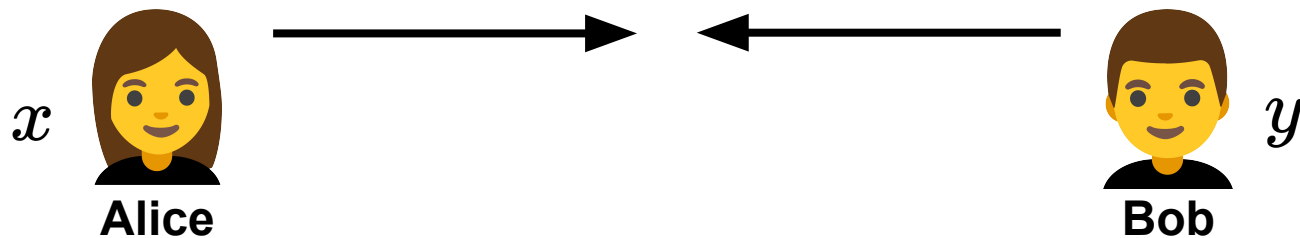


Secure Computation

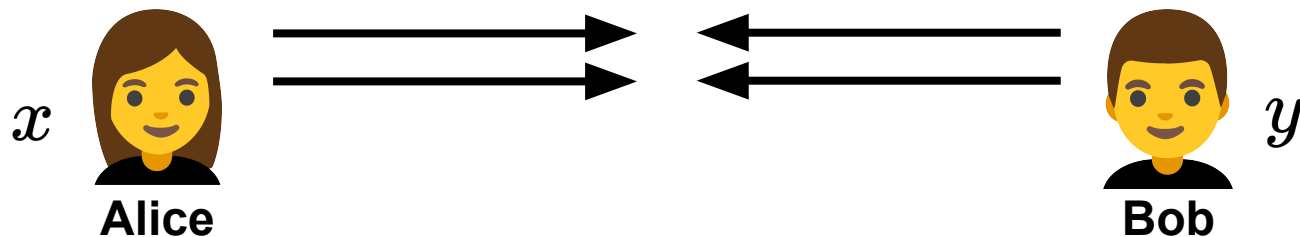
Alice learns y 😞



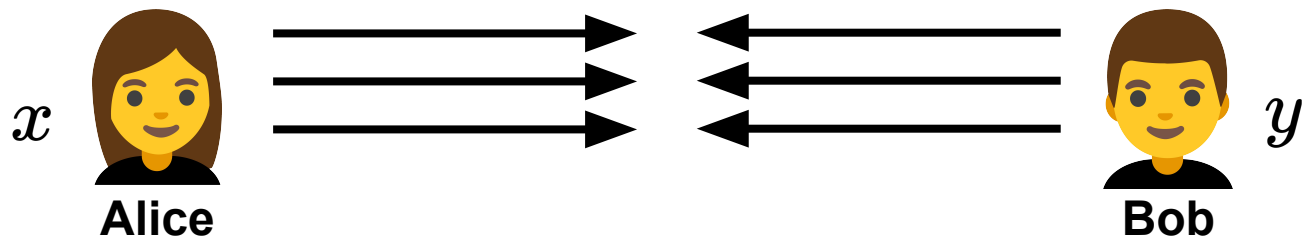
Secure Computation



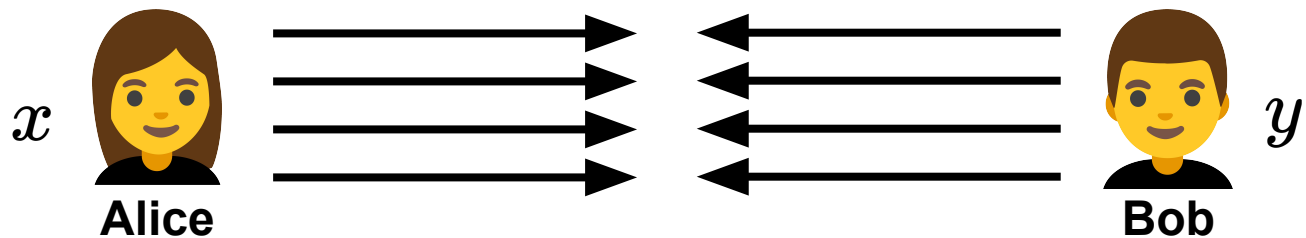
Secure Computation



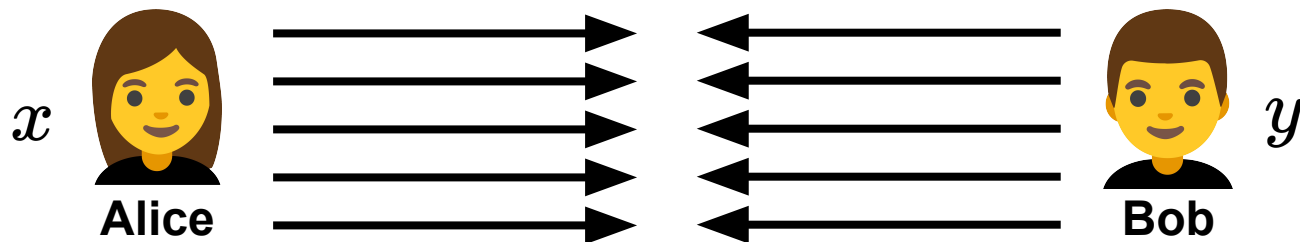
Secure Computation



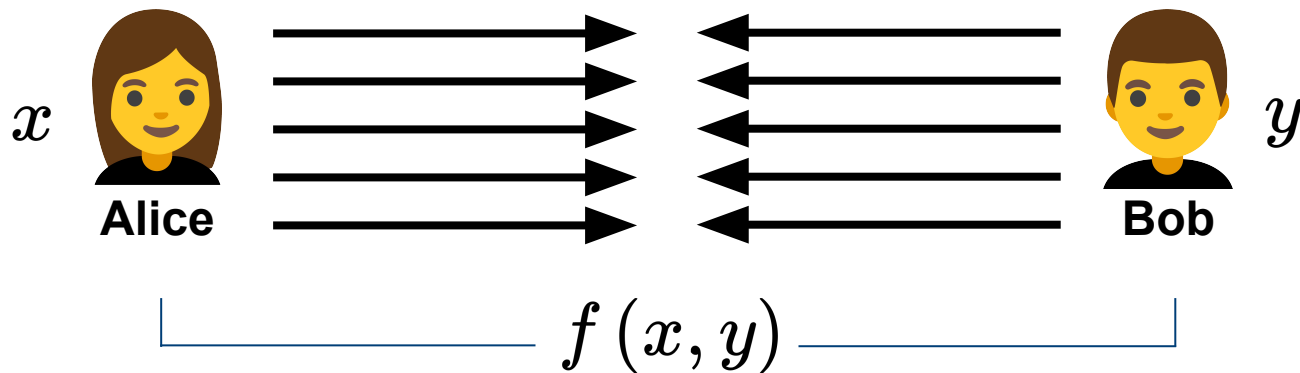
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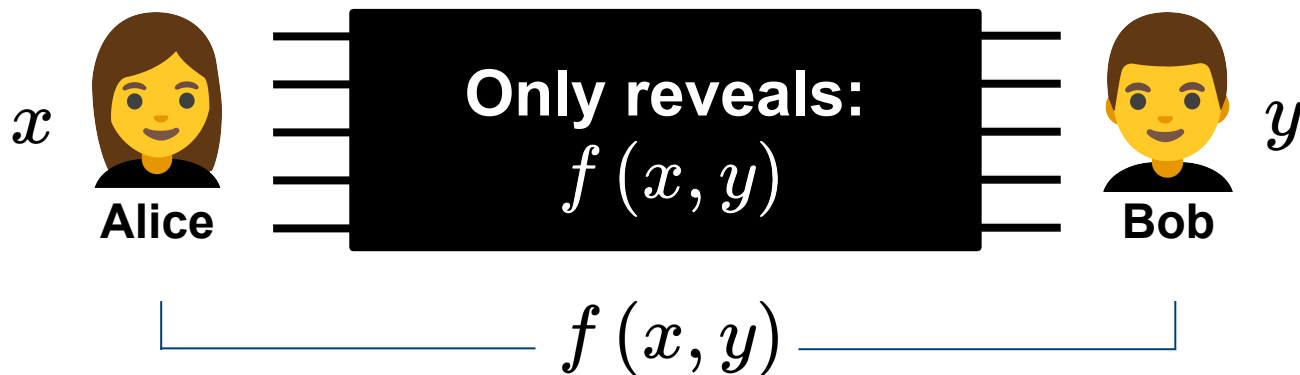
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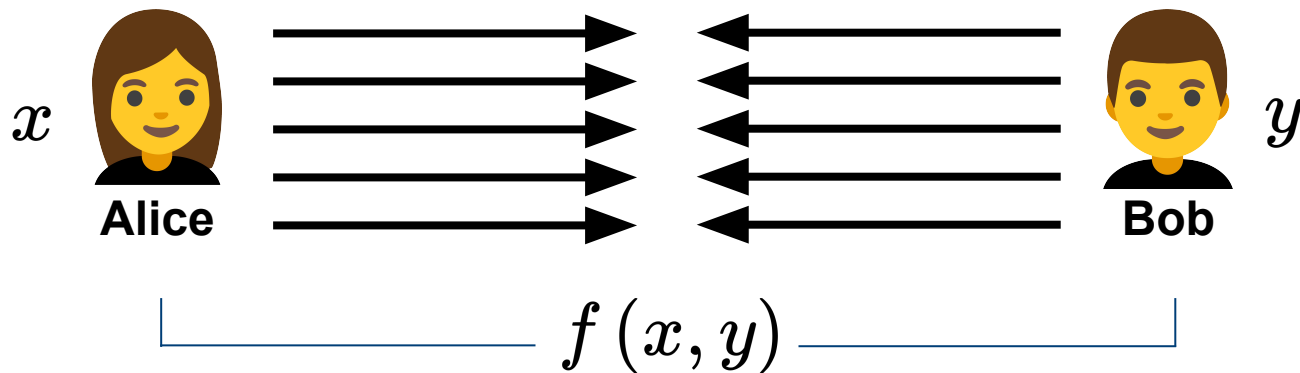
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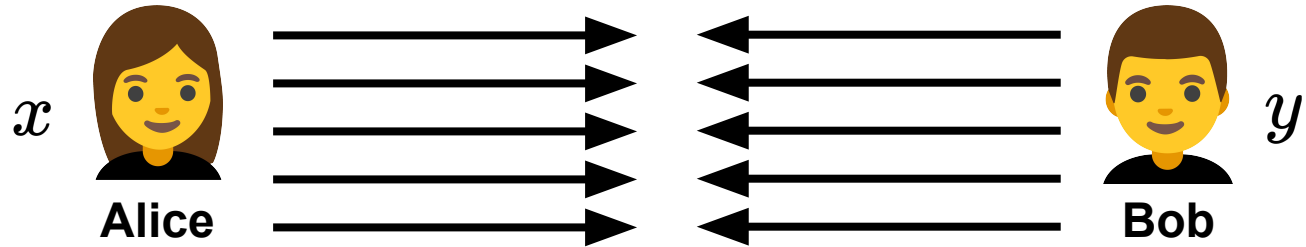


Secure Computation

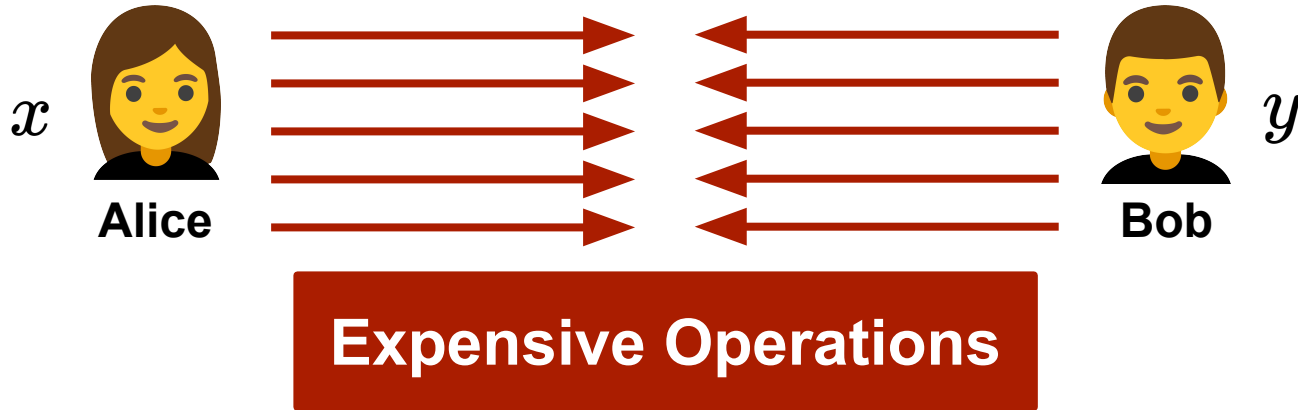


The Preprocessing Model

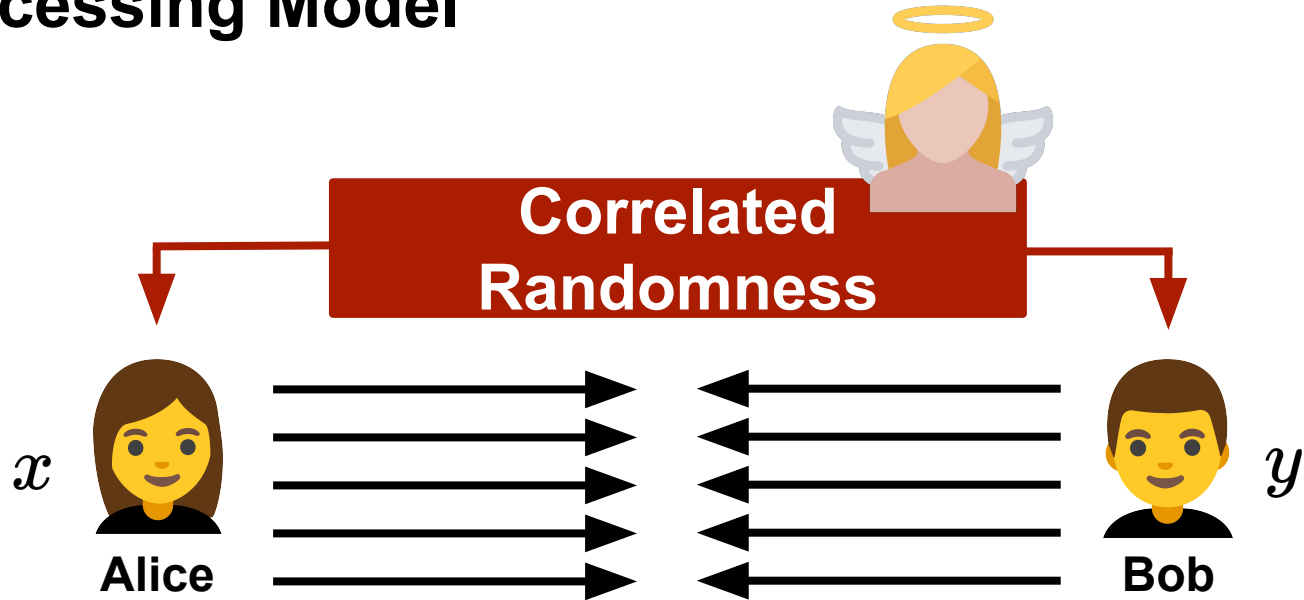
Preprocessing Model



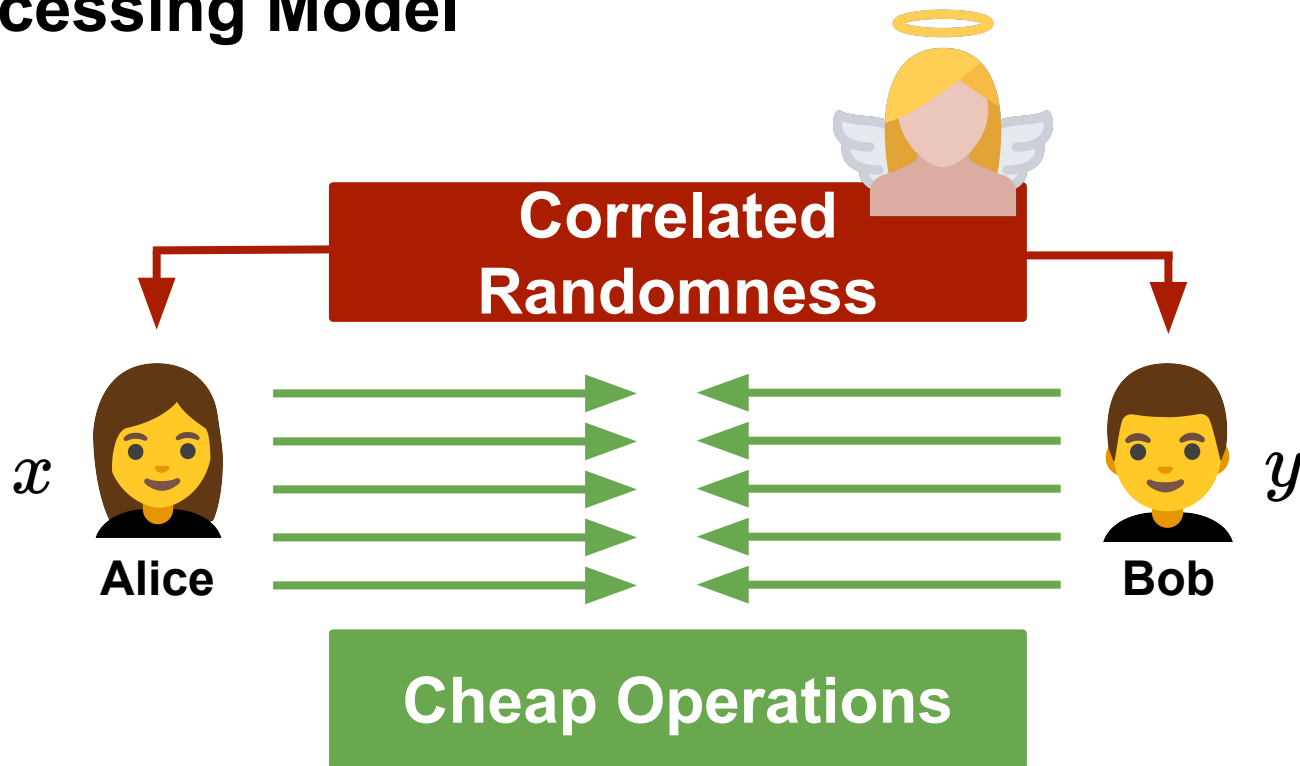
Preprocessing Model



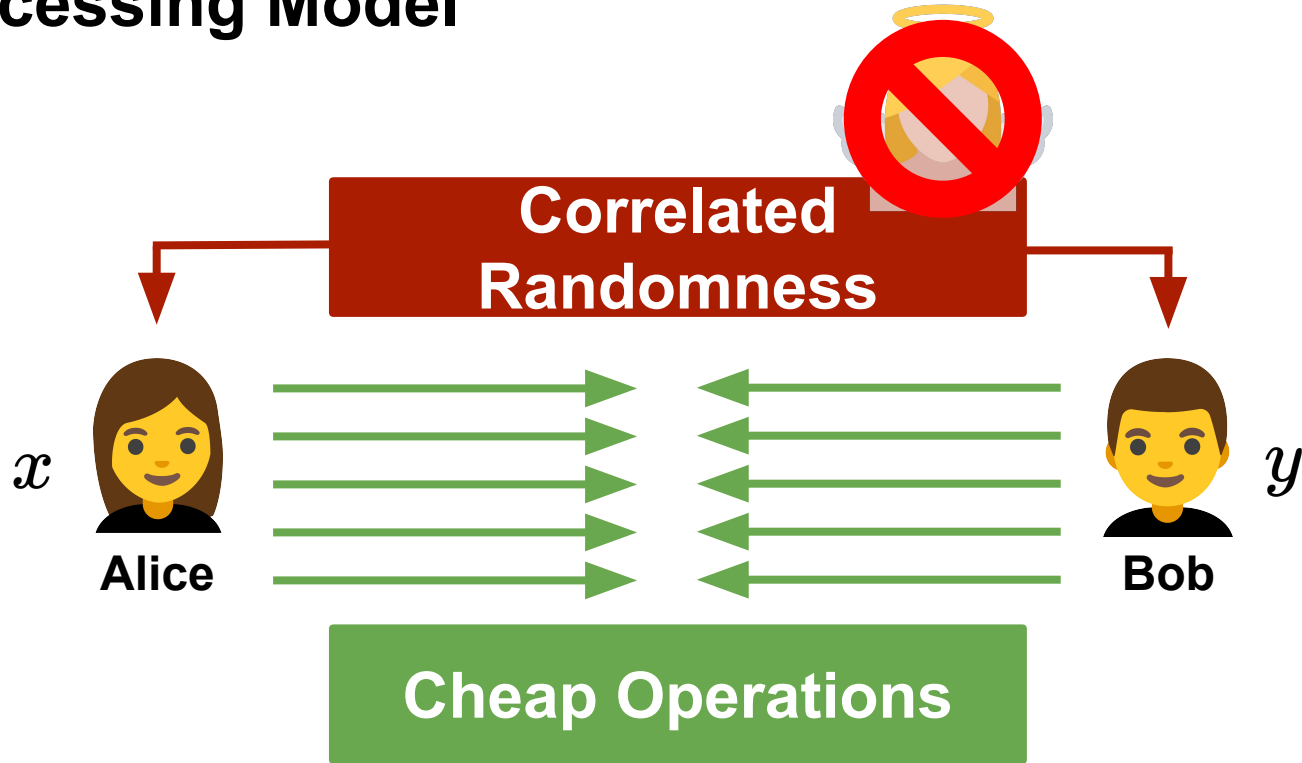
Preprocessing Model



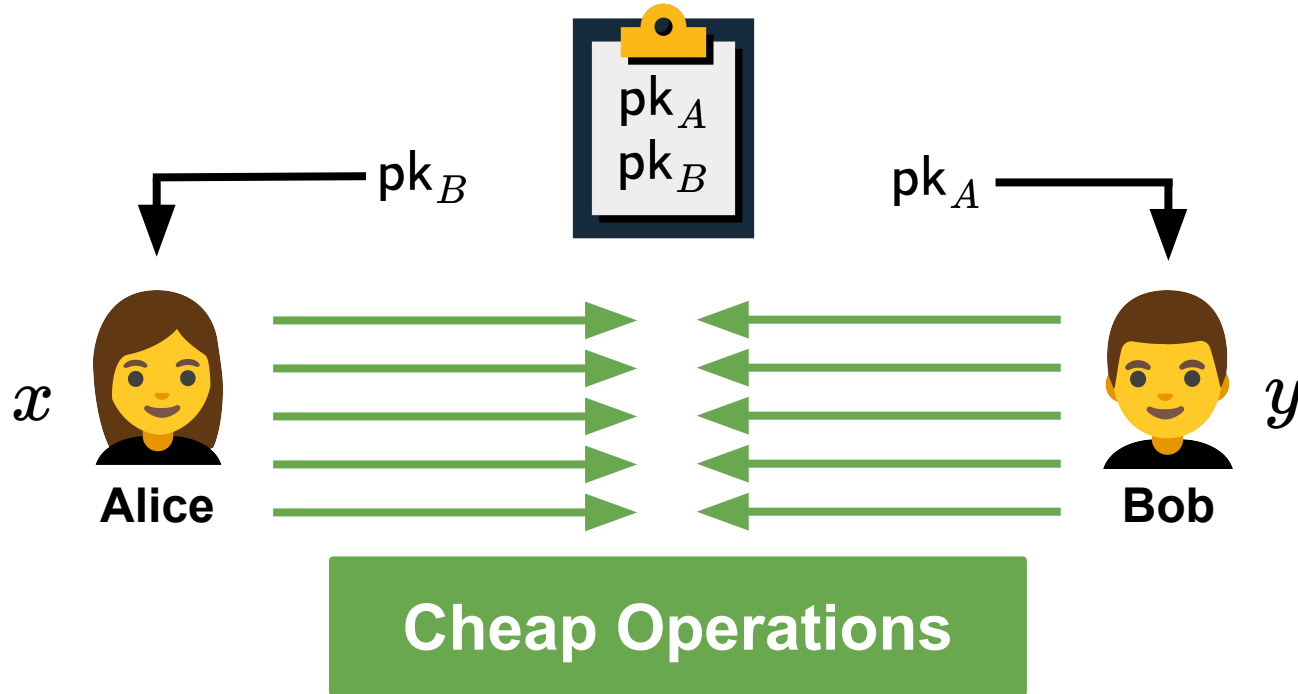
Preprocessing Model



Preprocessing Model



Preprocessing Model with a Public-Key Setup



This talk: Fast oblivious transfer with QuietOT

Overview

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Overview

- **Background on oblivious transfer**

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Overview

- **Background on oblivious transfer**
- **Background on OT extension**

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- **Background on oblivious transfer**
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- **QuietOT framework**

This talk: Fast oblivious transfer with QuietOT

Overview

- **Background on oblivious transfer**
- **Background on OT extension**
- **QuietOT framework**
- **Evaluation**

Oblivious Transfer

Oblivious Transfer



Alice



Bob

Oblivious Transfer



Alice

(m_0, m_1)



Bob

b

Oblivious Transfer



Alice

(m_0, m_1)

Wants: \perp



Bob

b

Wants: m_b

Oblivious Transfer



Wants: \perp

Wants: m_b

Oblivious Transfer for secure computation



Alice



Bob

Oblivious Transfer for secure computation



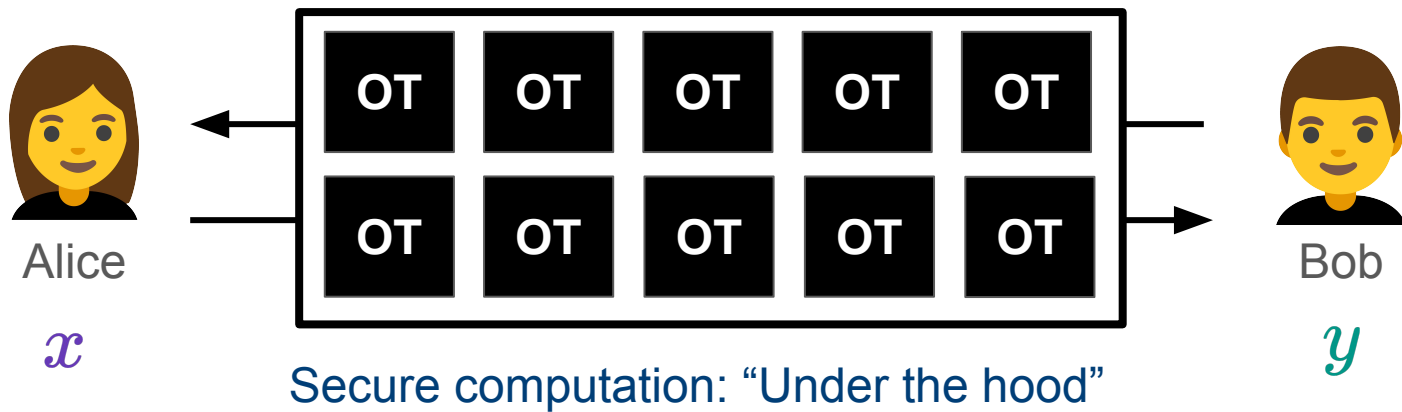
Oblivious Transfer for secure computation



Wants: \perp

Wants: $f(x, y)$

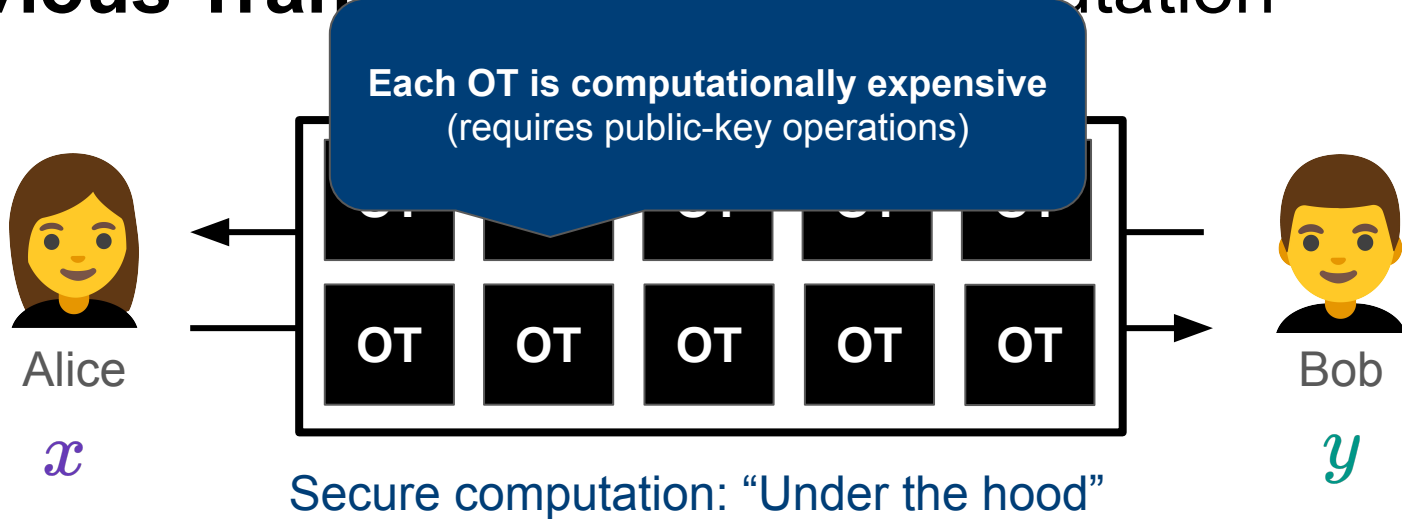
Oblivious Transfer for secure computation



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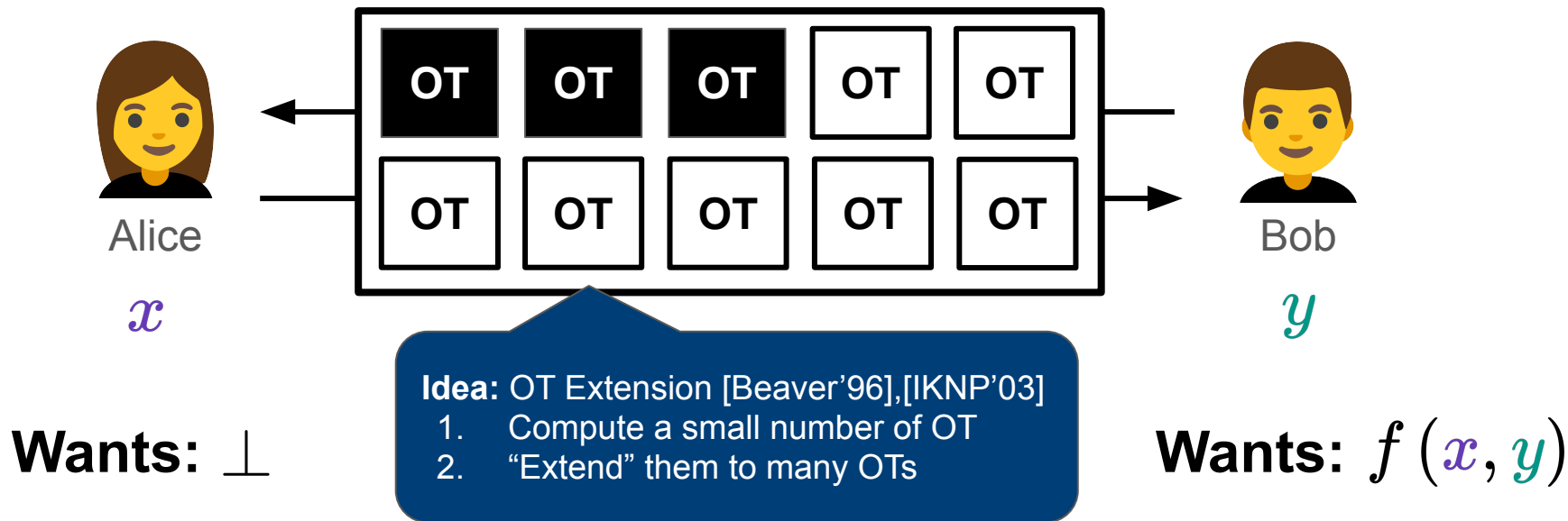
Oblivious Transfer for secure computation



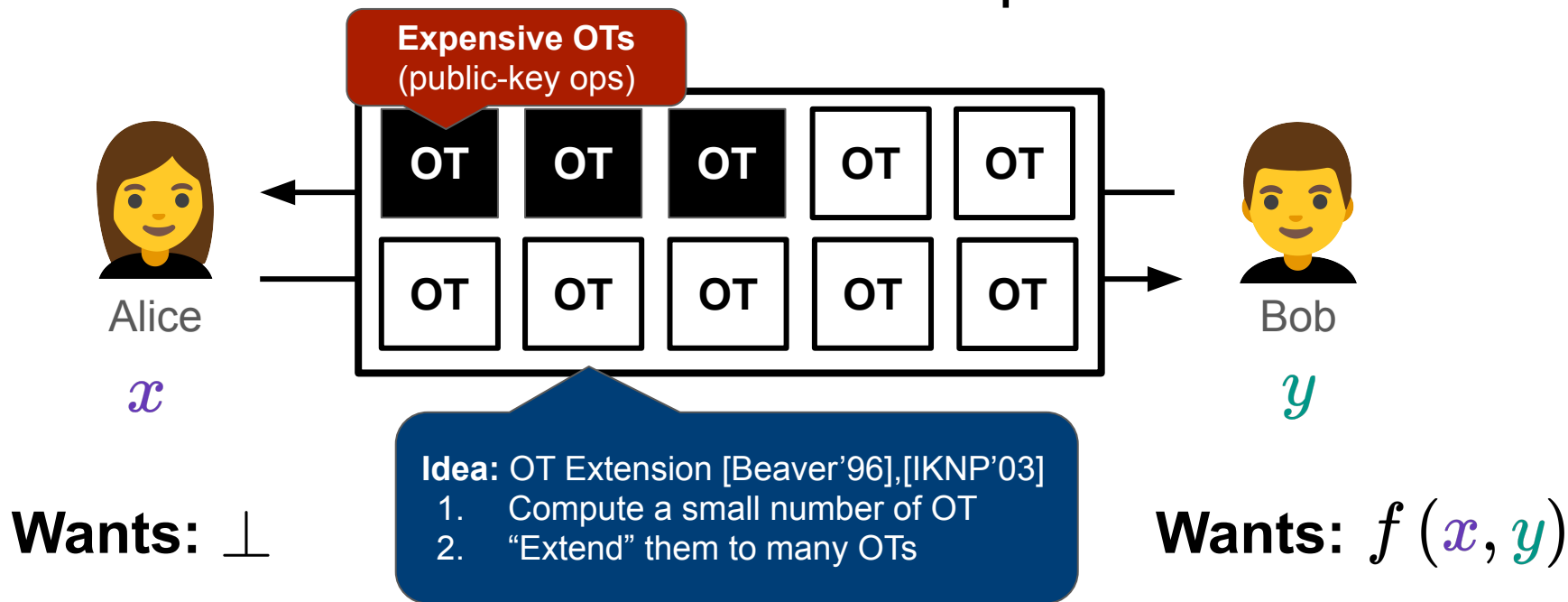
Wants: \perp

Wants: $f(x, y)$

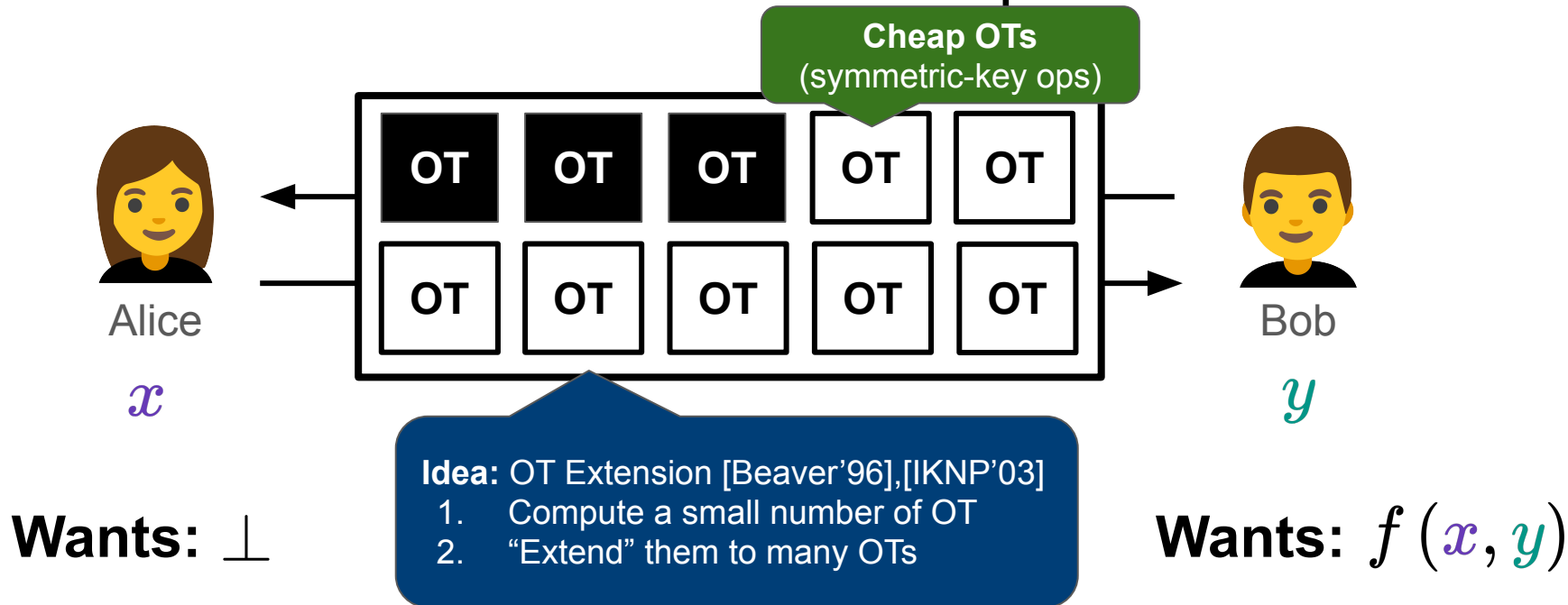
Oblivious Transfer for secure computation



Oblivious Transfer for secure computation



Oblivious Transfer for secure computation



OT Extension

OT Extension

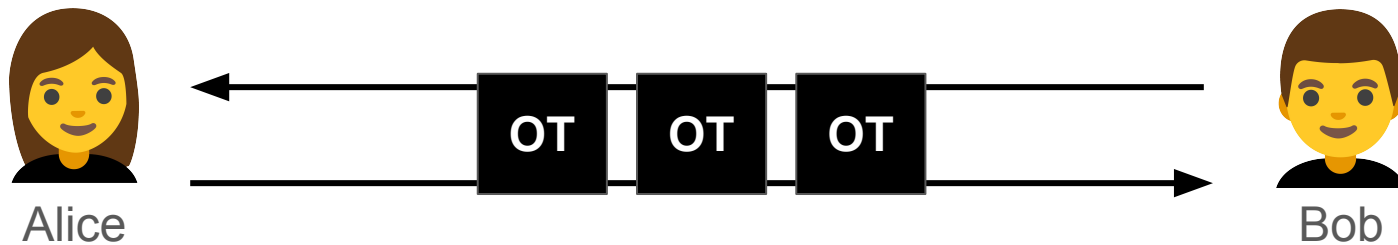


Alice

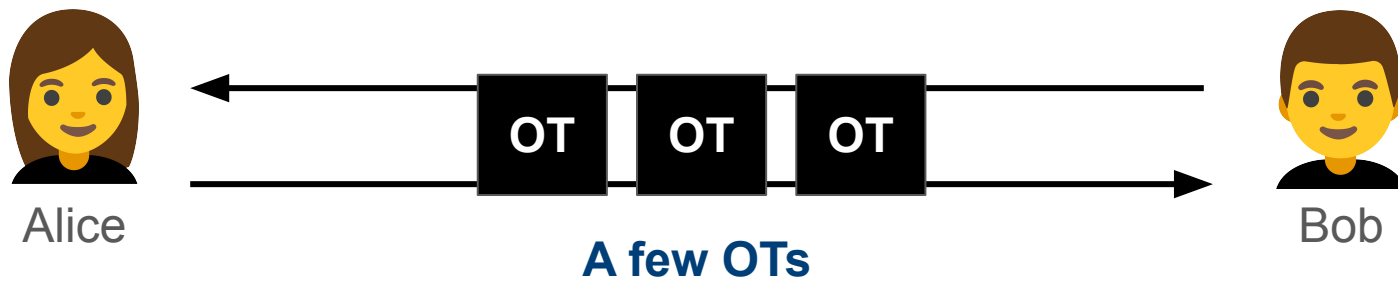


Bob

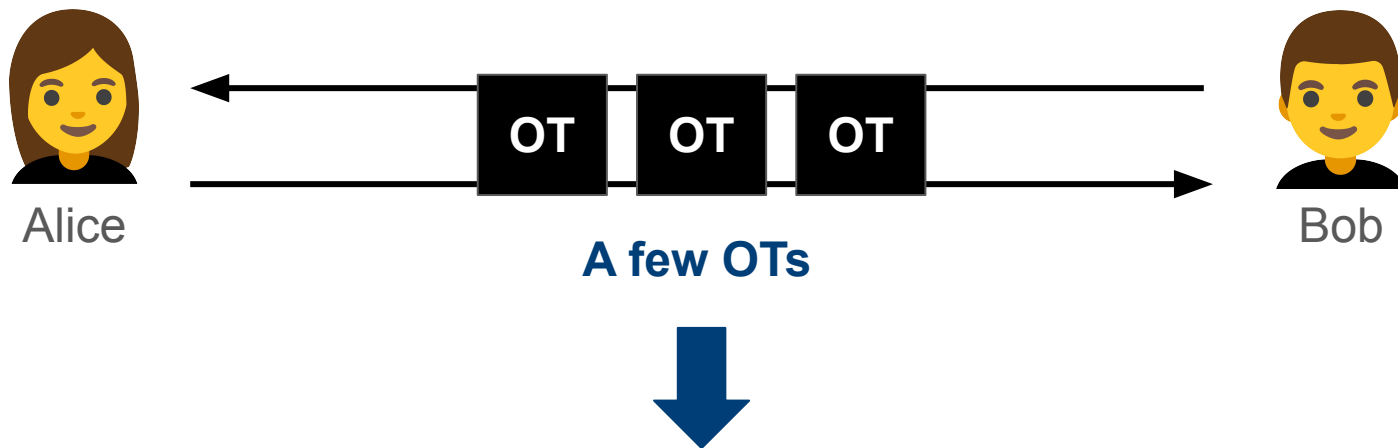
OT Extension



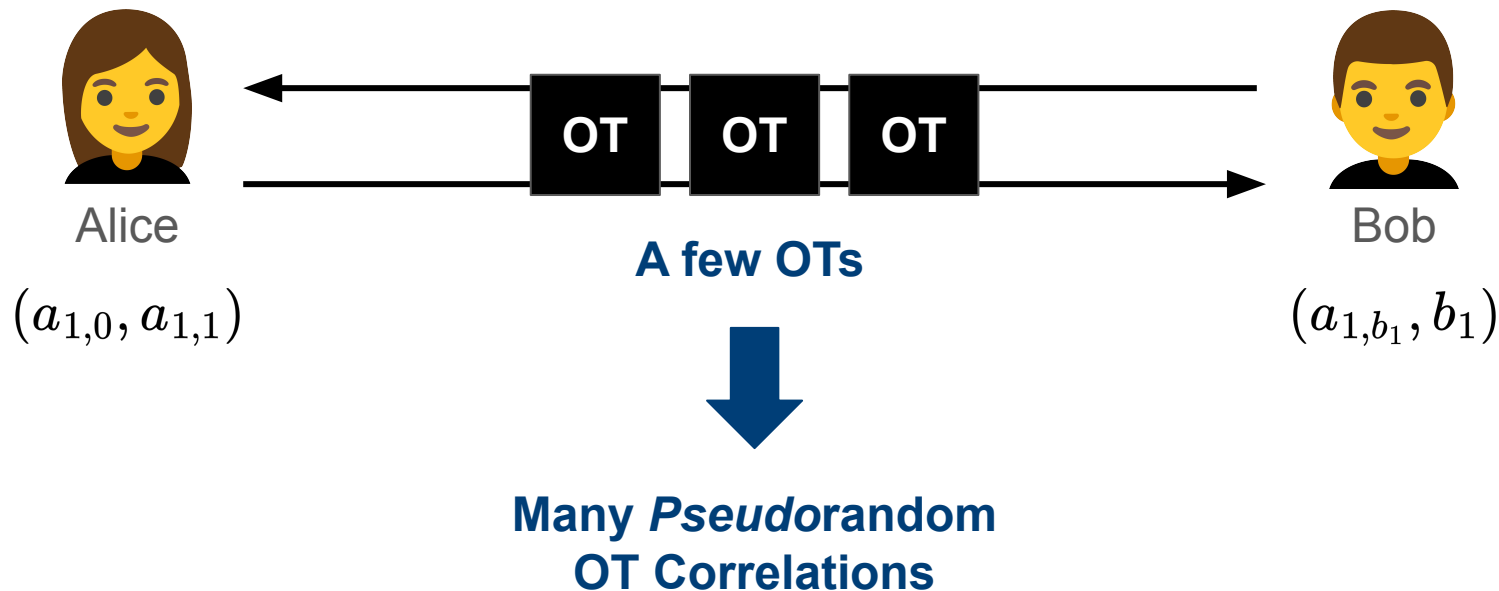
OT Extension



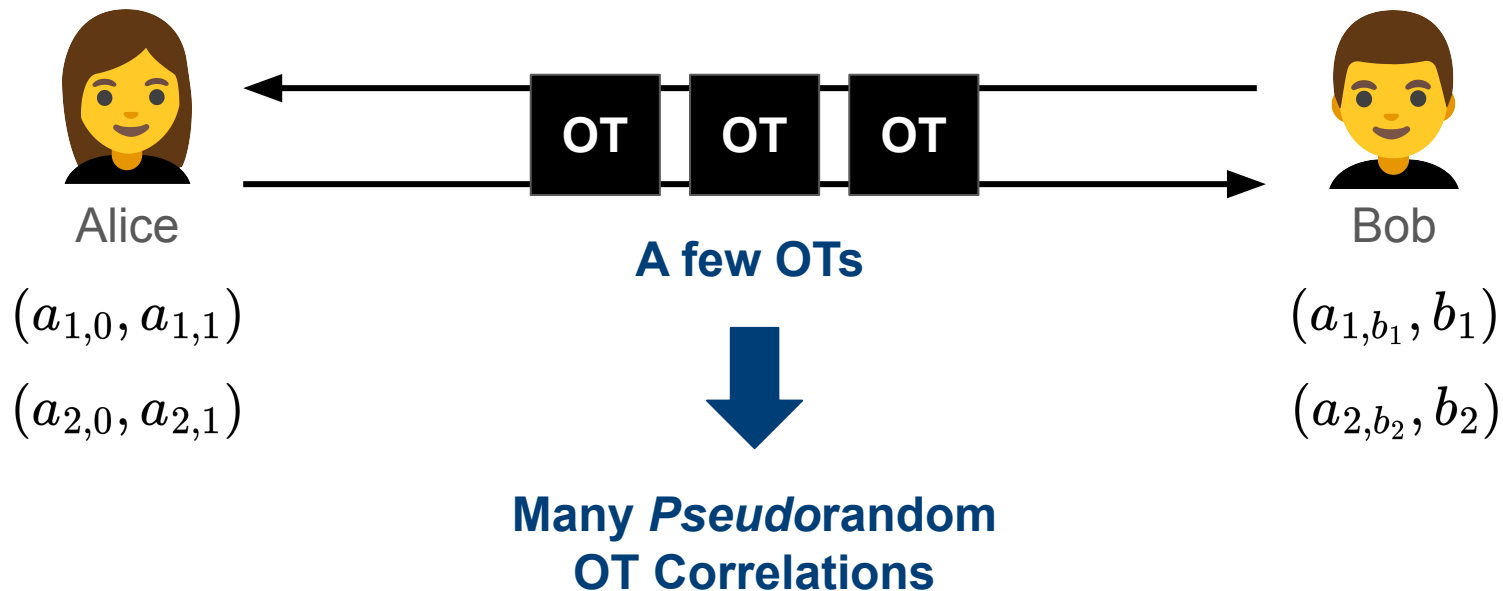
OT Extension



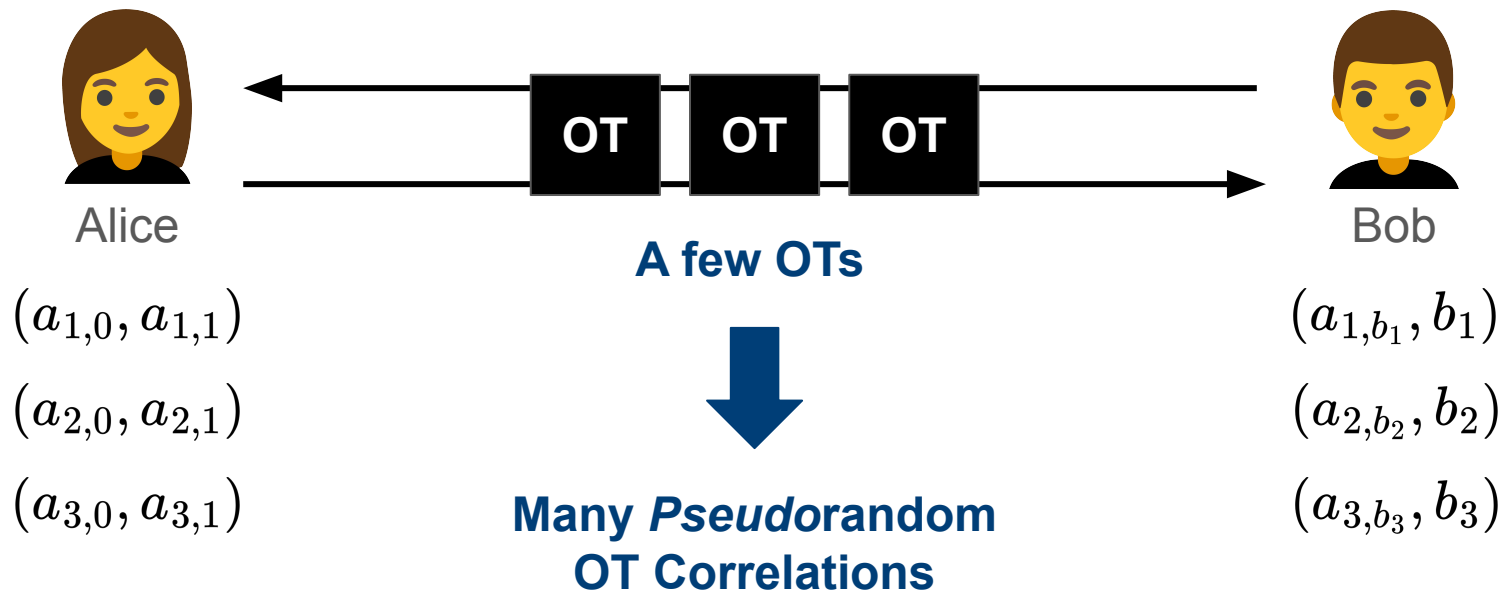
OT Extension



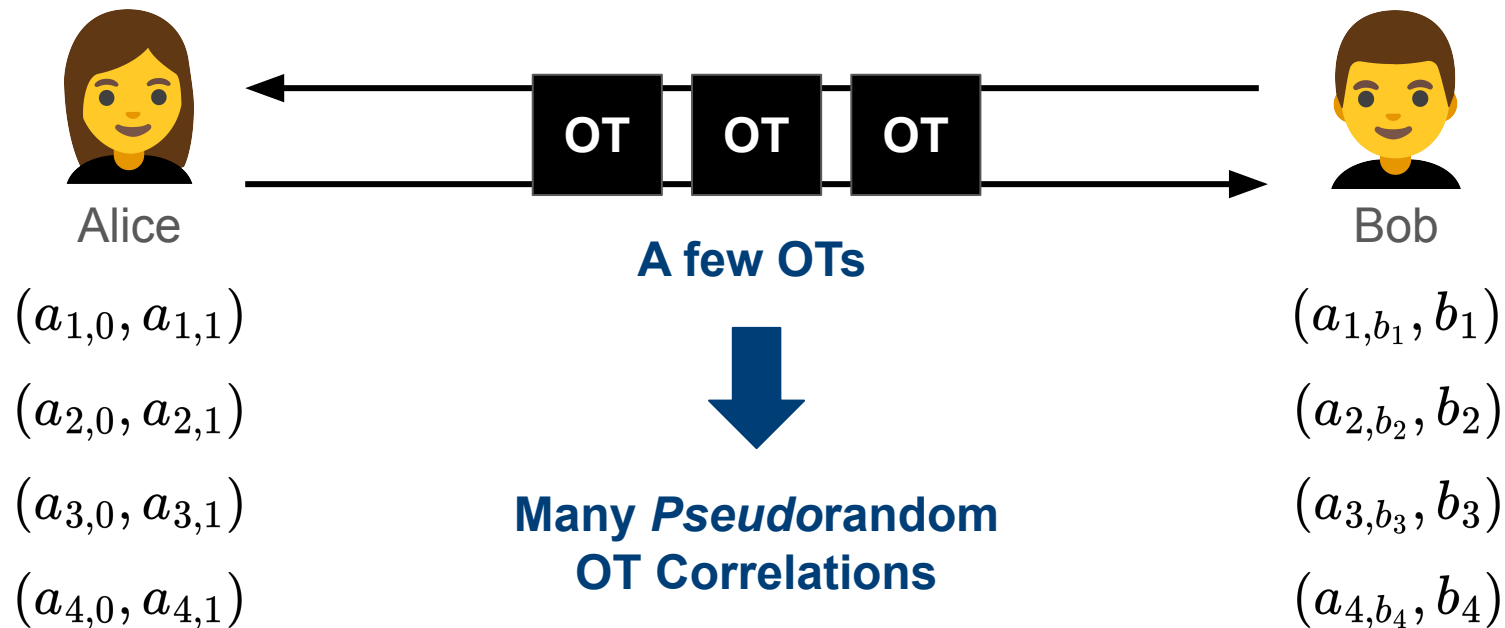
OT Extension



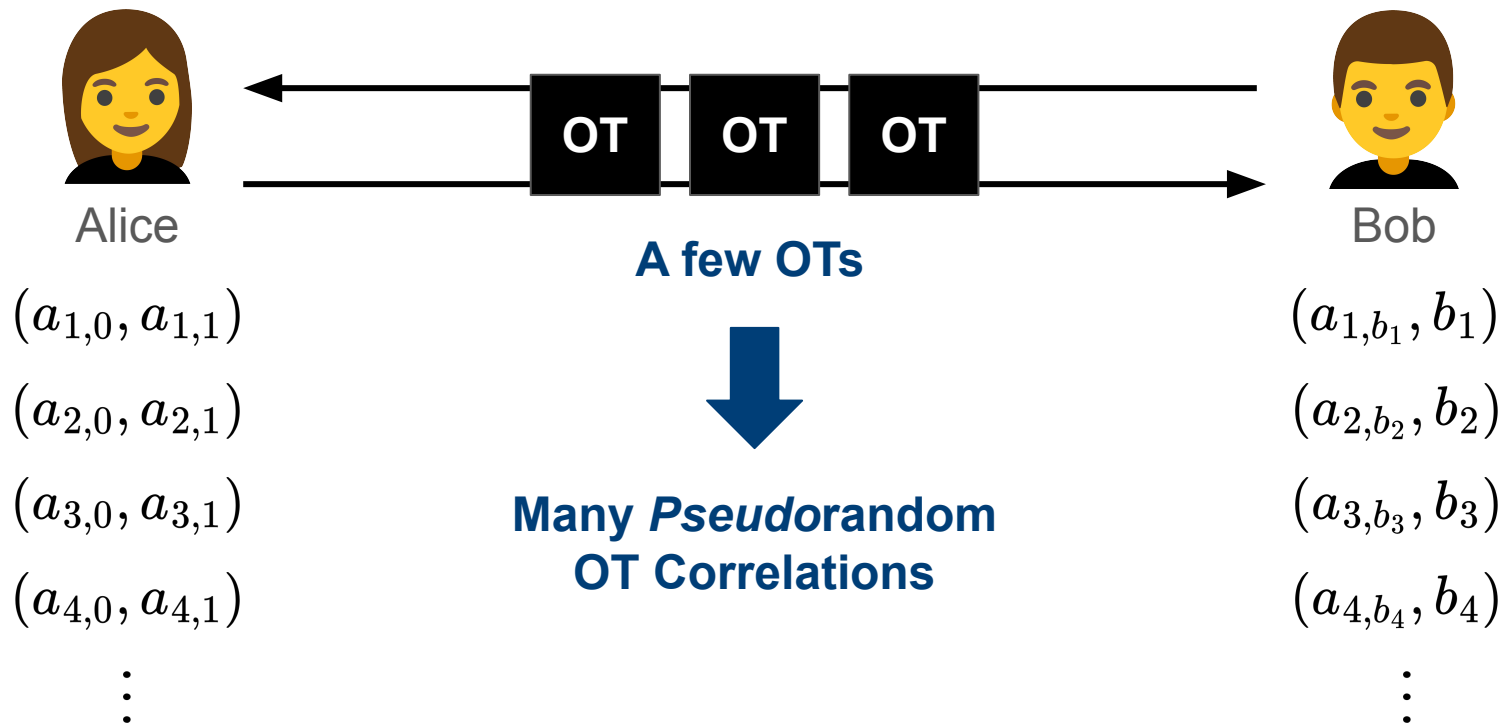
OT Extension



OT Extension



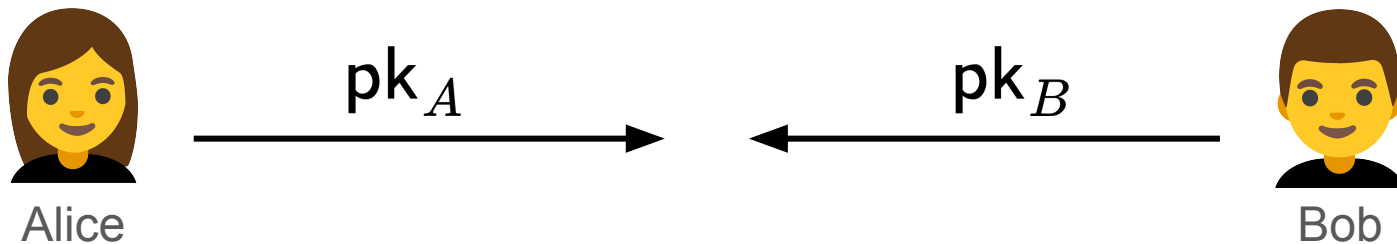
OT Extension



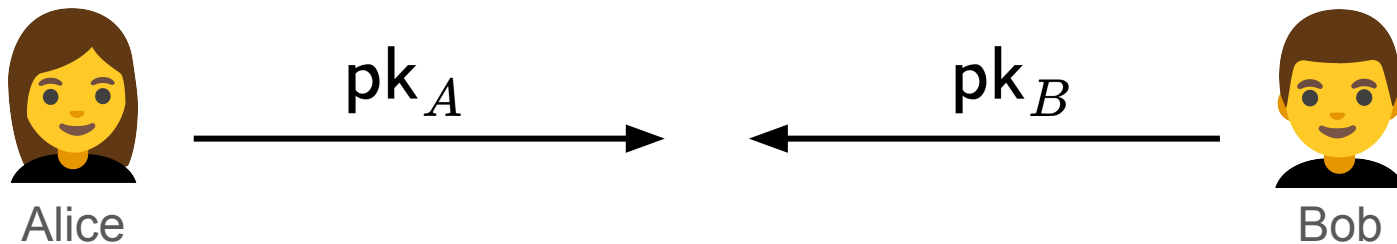
OT Extension with a public-key setup



OT Extension **with a public-key setup**

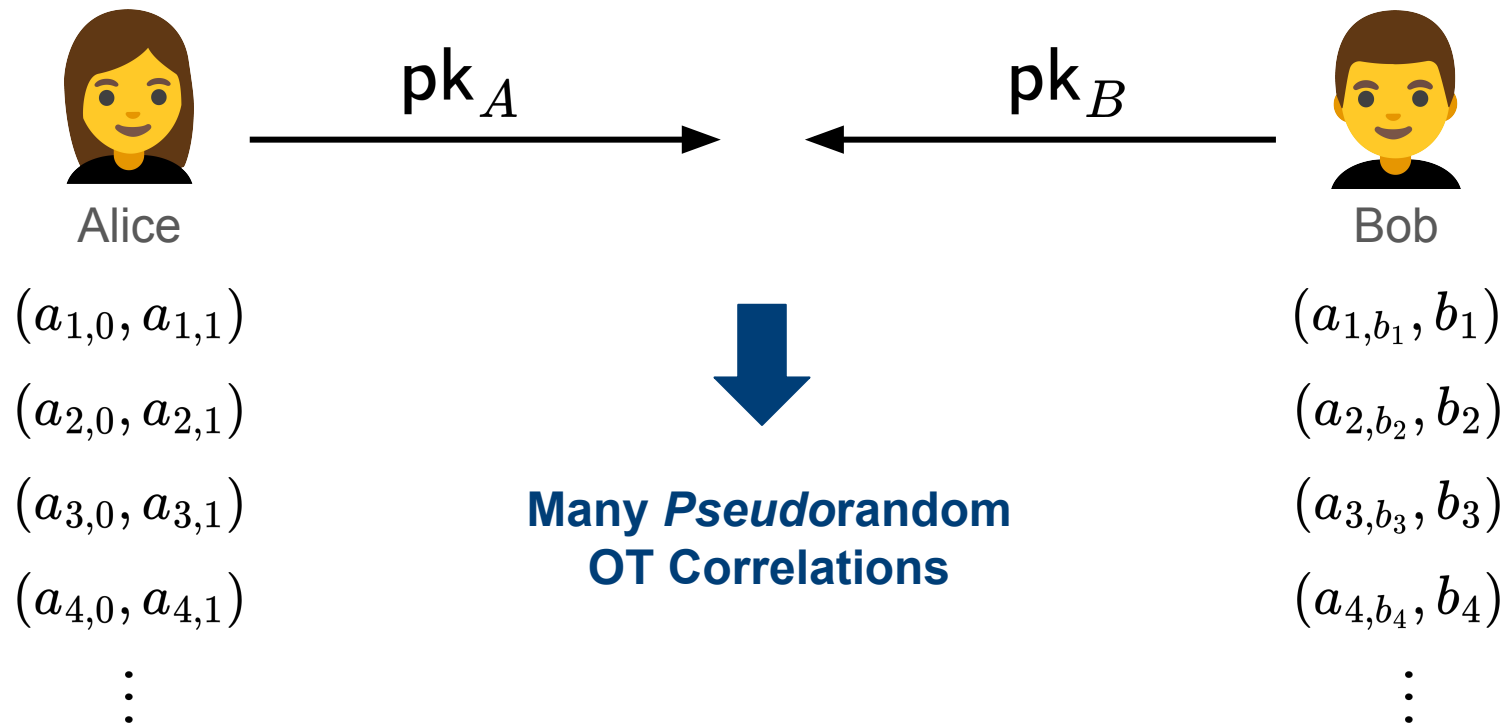


OT Extension **with a public-key setup**

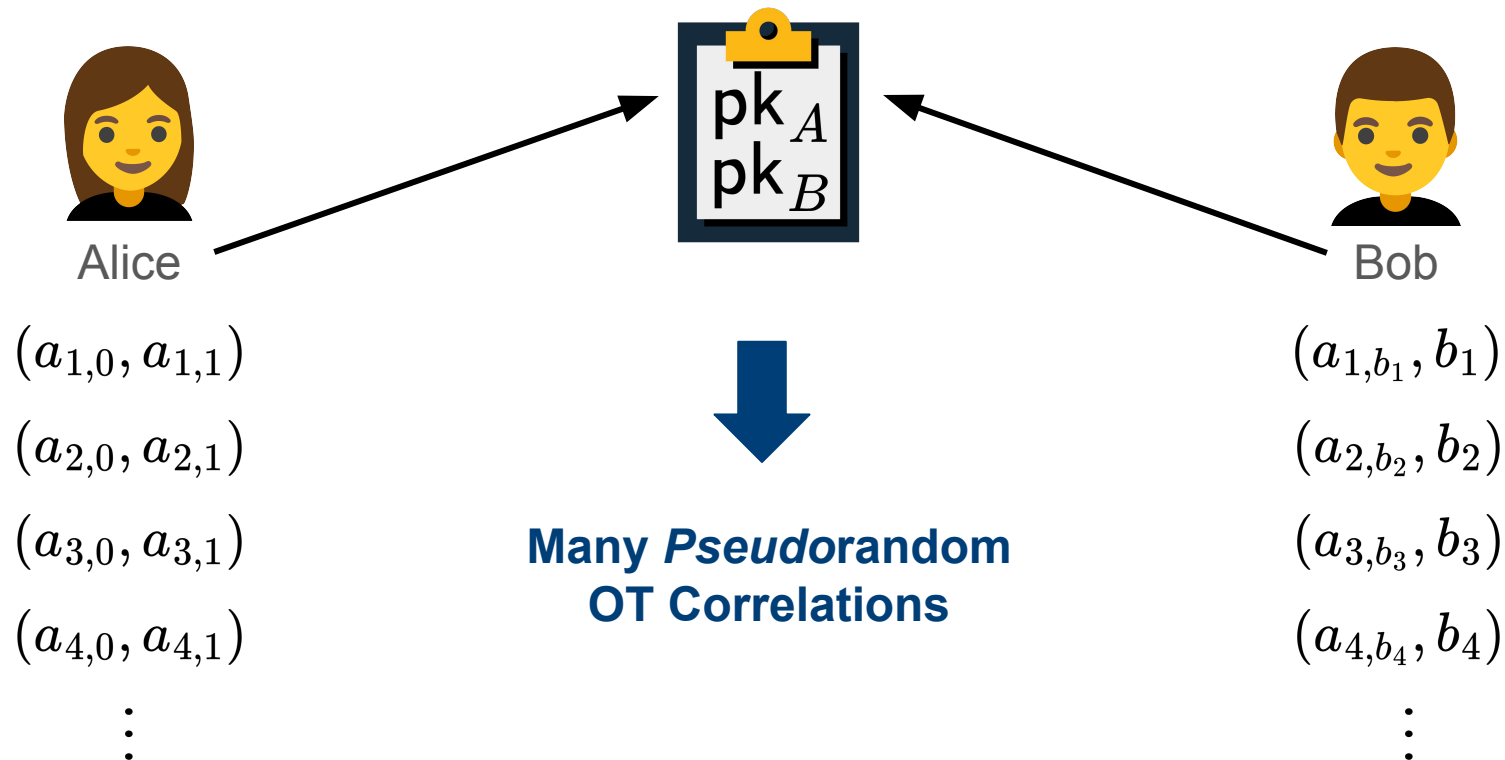


**Many *Pseudorandom*
OT Correlations**

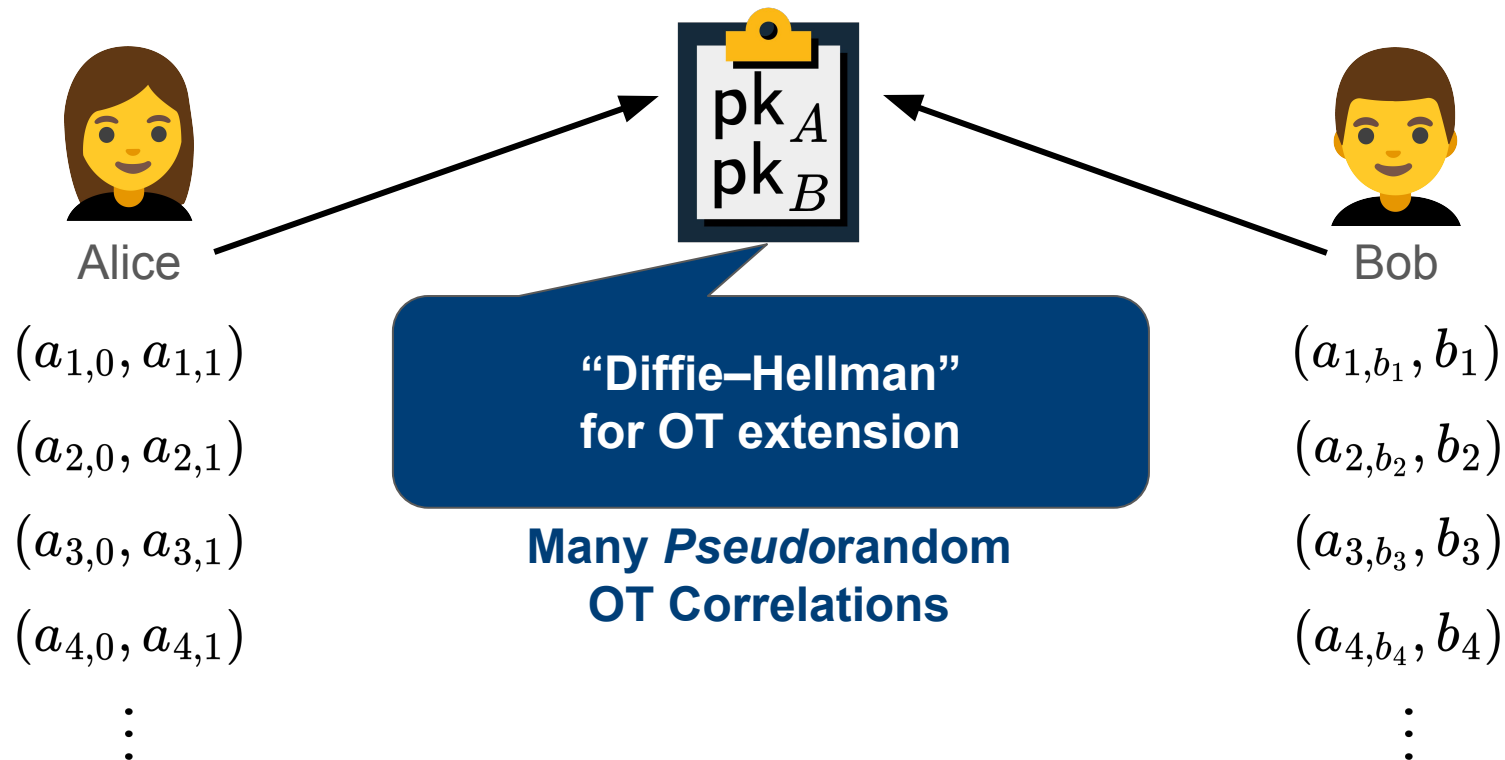
OT Extension with a public-key setup



OT Extension with a public-key setup

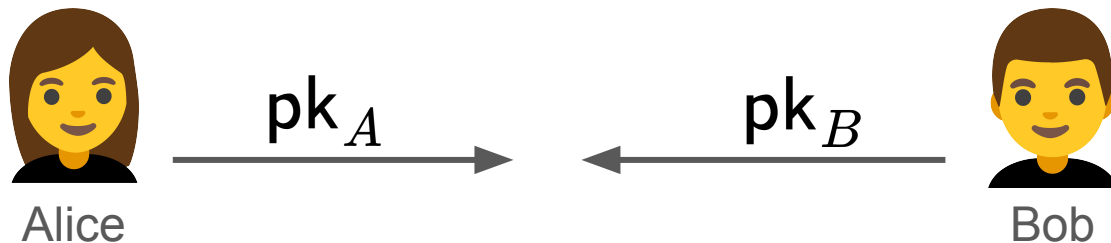


OT Extension with a public-key setup

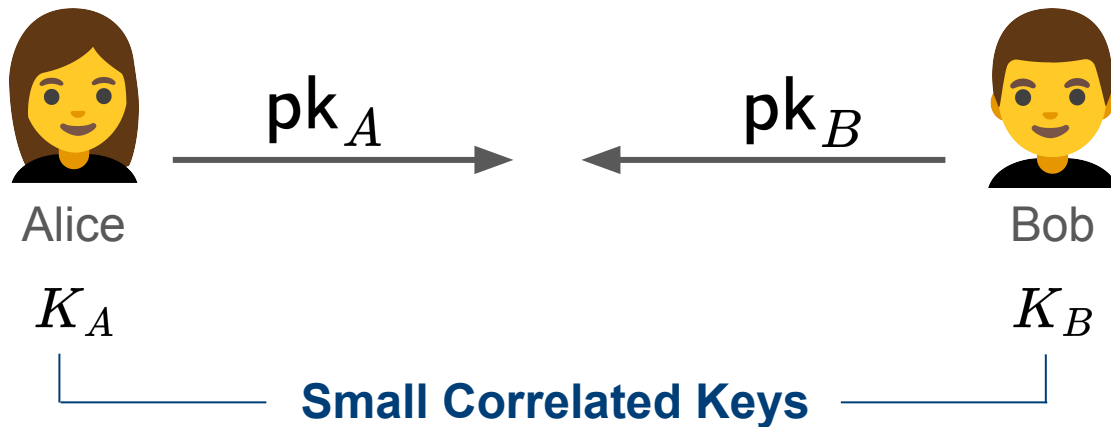


QuietOT Framework

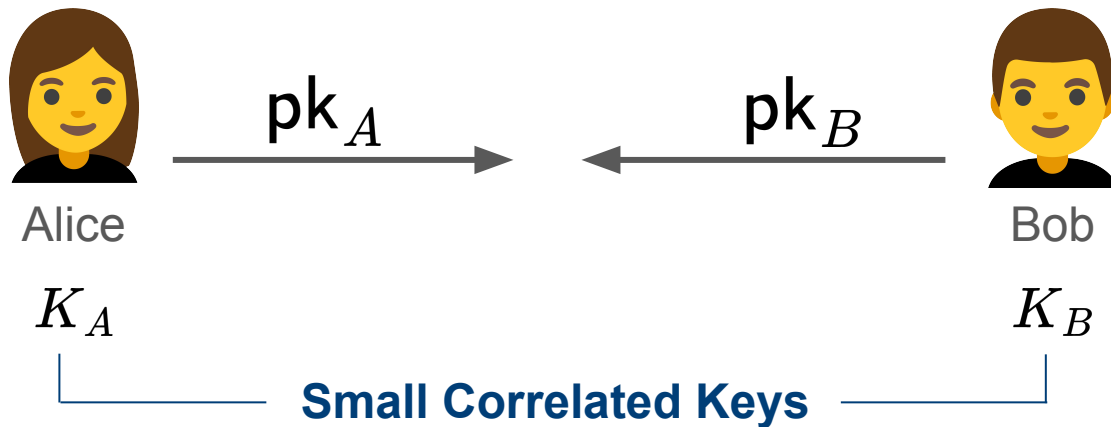
QuietOT: Communication model and syntax



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$((a_{1,0}, a_{1,1}), \dots, (a_{n,0}, a_{n,1})) \leftarrow \text{Extend}_A(K_A)$
 $((a_{1,b_1}, b_1), \dots, (a_{n,b_n}, b_n)) \leftarrow \text{Extend}_B(K_B)$

} **Locally generate many pseudorandom “OTs”**

QuietOT: The main ingredients

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**CPRF for
Inner-Products**

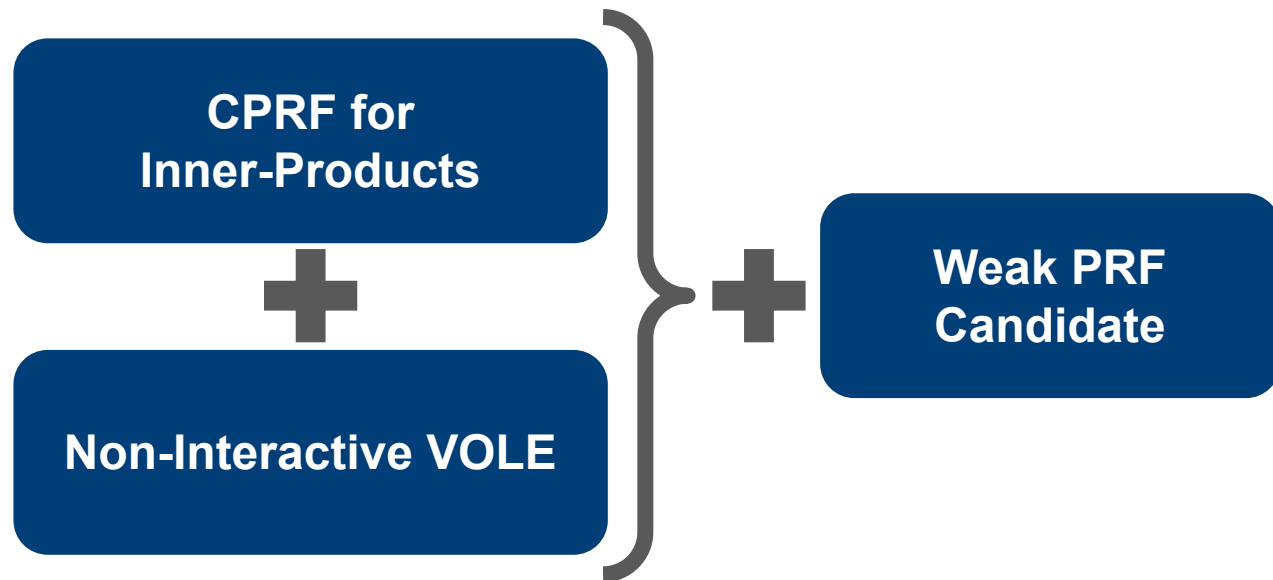
QuietOT: The main ingredients

**CPRF for
Inner-Products**

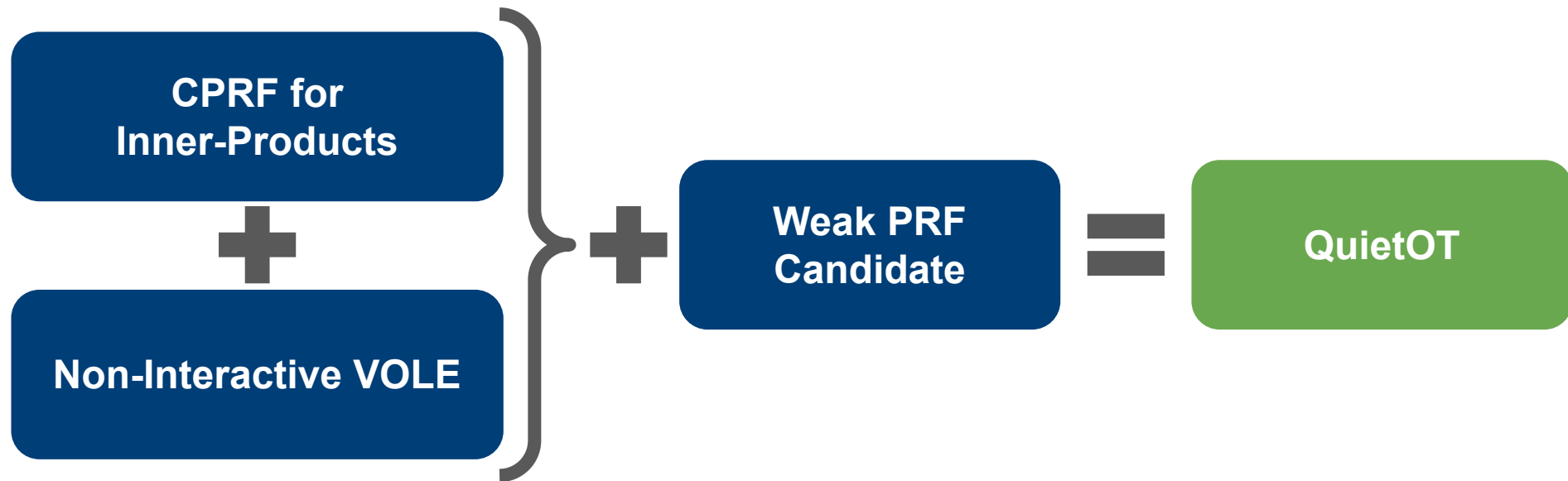


Non-Interactive VOLE

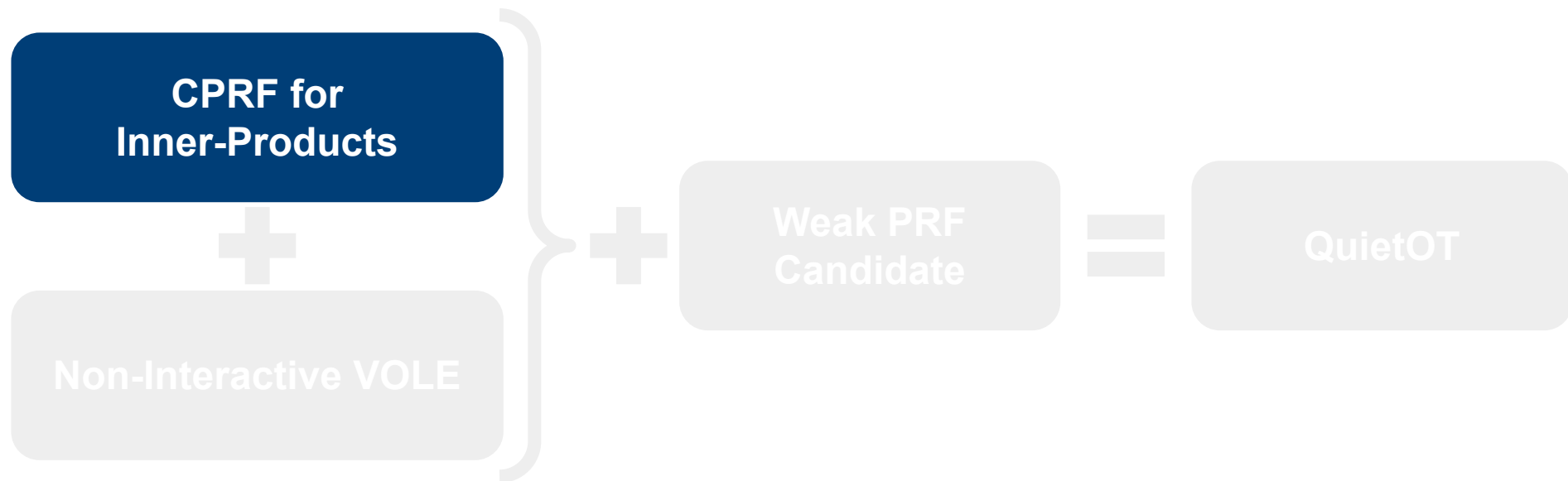
QuietOT: The main ingredients



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Ingredient I: CPRF for Inner-Products

Constrained Pseudorandom Function (CPRF) [BW'13][KPTZ'13][BGI'14]

CPRFs have an additional **constrain** functionality for a class of circuits C :

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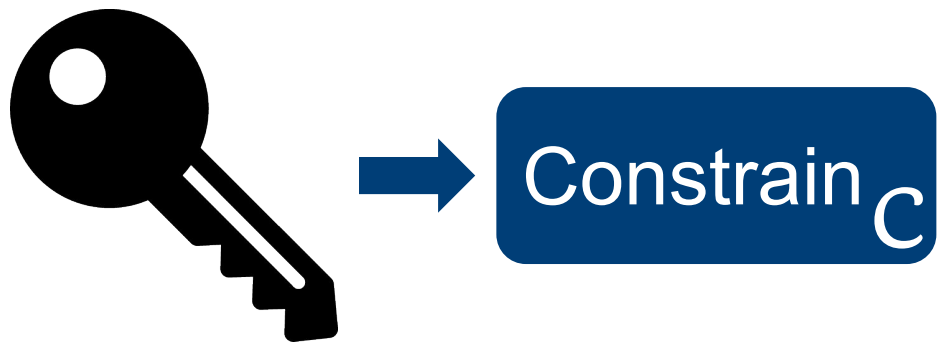


Master PRF Key

Ingredient I: CPRF for Inner-Products

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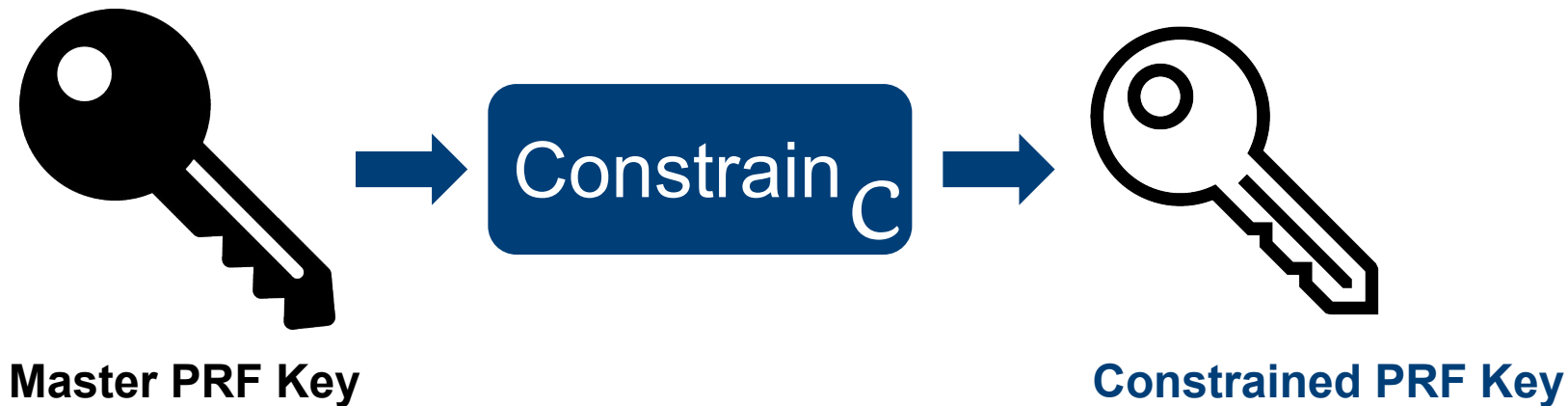


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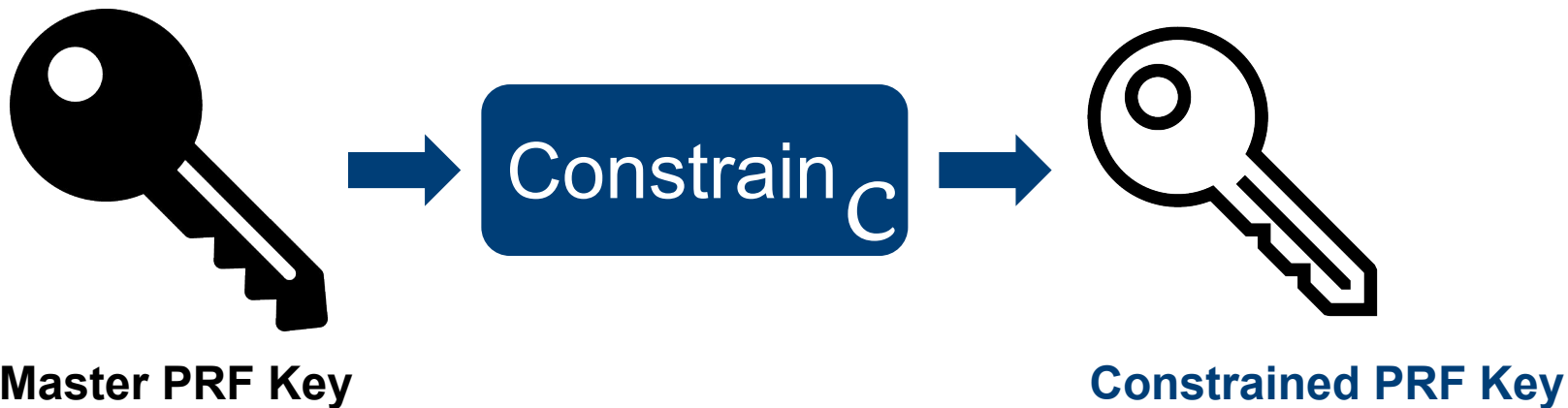
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Ingredient I: CPRF for Inner-Products

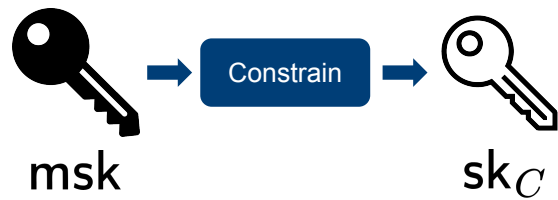
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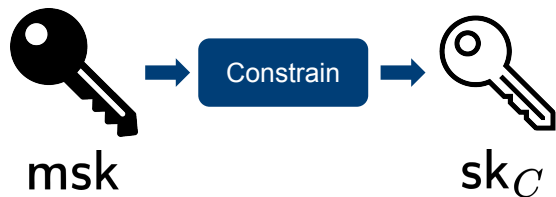


Constrained key  can be used to evaluate PRF (, x) for all $x \in \mathcal{X}$ where $C(x) = 0$

Ingredient I: CPRF for Inner-Products

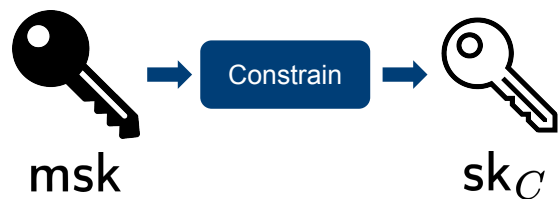


Ingredient I: CPRF for Inner-Products



$$C(x) = \begin{cases} 0 & \text{authorized} \\ 1 & \text{unauthorized} \end{cases}$$

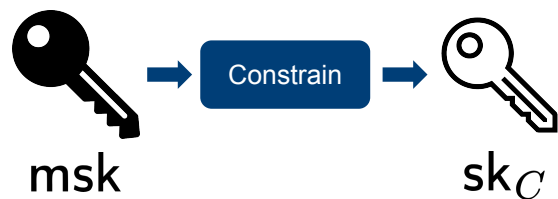
Ingredient I: CPRF for Inner-Products



$$C(x) = \begin{cases} 0 & \text{authorized} \\ 1 & \text{unauthorized} \end{cases}$$

Correctness: If $C(x) = 0$ then $\text{PRF}(msk, x) = \text{PRF}(sk_C, x)$

Ingredient I: CPRF for Inner-Products



$$C(x) = \begin{cases} 0 & \text{authorized} \\ 1 & \text{unauthorized} \end{cases}$$

Correctness: If $C(x) = 0$ then $\text{PRF}(msk, x) = \text{PRF}(sk_C, x)$

Pseudorandomness: If $C(x) \neq 0$ then $\text{PRF}(msk, x)$ is pseudorandom given sk_C

Ingredient I: CPRF for Inner-Products

For efficiency: Use CPRF with inner-product predicate

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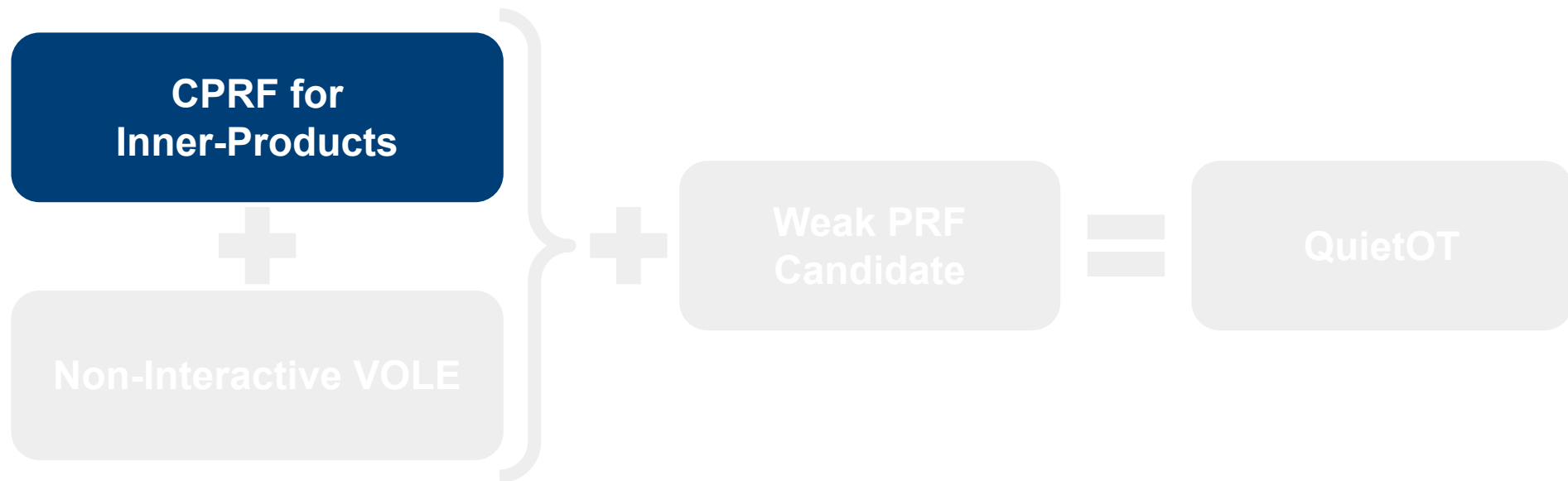
Ingredient I: CPRF for Inner-Products

For efficiency: Use CPRF with inner-product predicate

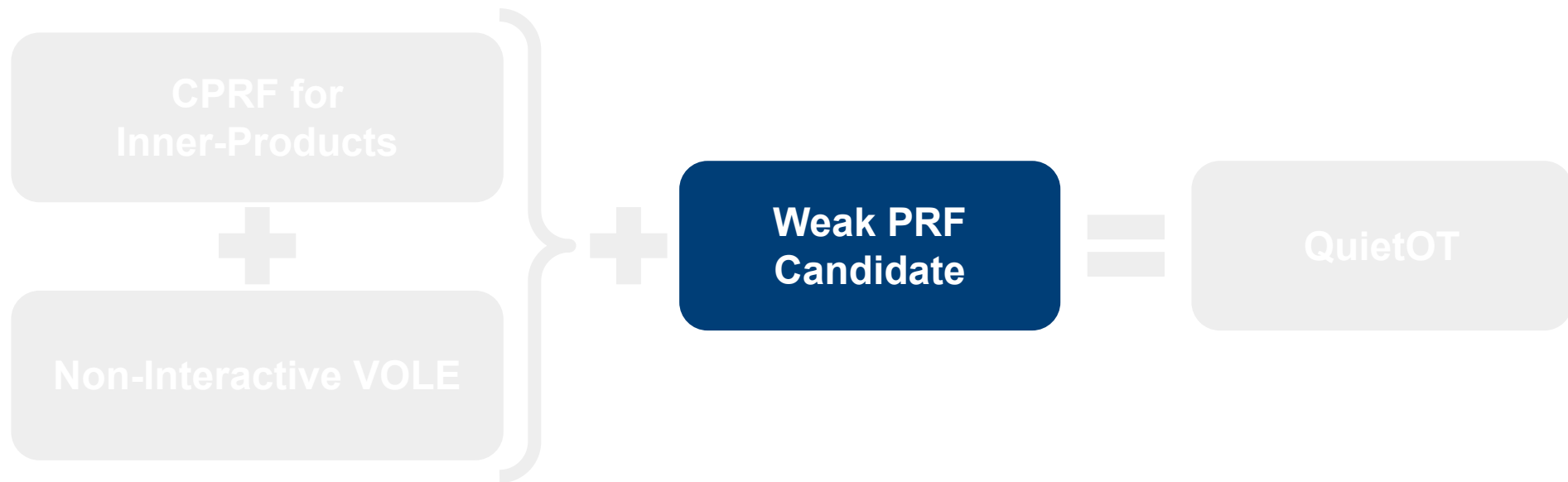
$$C(\mathbf{x}) = \langle \mathbf{z}, \mathbf{x} \rangle \in \mathcal{R} \text{ where } \mathbf{z}, \mathbf{x} \in \mathcal{R}^\ell$$

We use the random-oracle based CPRF construction of [S'24]

QuietOT: The main ingredients



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Ingredient II: “Inner-Product Membership” PRF

BIPSW weak PRF candidate: [BIPSW'18]

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$$f_{\mathbf{k}}(\mathbf{x}) := \lceil \langle \mathbf{k}, \mathbf{x} \rangle \bmod 6 \rceil_2$$

Ingredient II: “Inner-Product Membership” PRF

BIPSW weak PRF candidate: [BIPSW'18]

$$f_{\mathbf{k}}(\mathbf{x}) := \left\lceil \underbrace{\langle \mathbf{k}, \mathbf{x} \rangle}_{\text{Just an inner product}} \bmod 6 \right\rceil_2$$

Just an inner product

Ingredient II: “Inner-Product Membership” PRF

BIPSW weak PRF candidate: [BIPSW'18]

$$f_{\mathbf{k}}(\mathbf{x}) := \underbrace{\lceil \langle \mathbf{k}, \mathbf{x} \rangle \bmod 6 \rceil}_2$$

Cannot be evaluated as an inner product

Ingredient II: “Inner-Product Membership” PRF

BIPSW weak PRF candidate: [BIPSW'18]

$$f_{\mathbf{k}}(\mathbf{x}) := \lceil \langle \mathbf{k}, \mathbf{x} \rangle \bmod 6 \rceil_2$$

Ingredient II: “Inner-Product Membership” PRF

BIPSW weak PRF candidate: [BIPSW'18]

$$f_{\mathbf{k}}(\mathbf{x}) := \lceil \langle \mathbf{k}, \mathbf{x} \rangle \bmod 6 \rceil_2$$

$$f_{\mathbf{k}}(\mathbf{x}) = 0 \iff \langle \mathbf{k}, \mathbf{x} \rangle \bmod 6 \in \{0, 1, 2\}$$

Ingredient II: “Inner-Product Membership” PRF

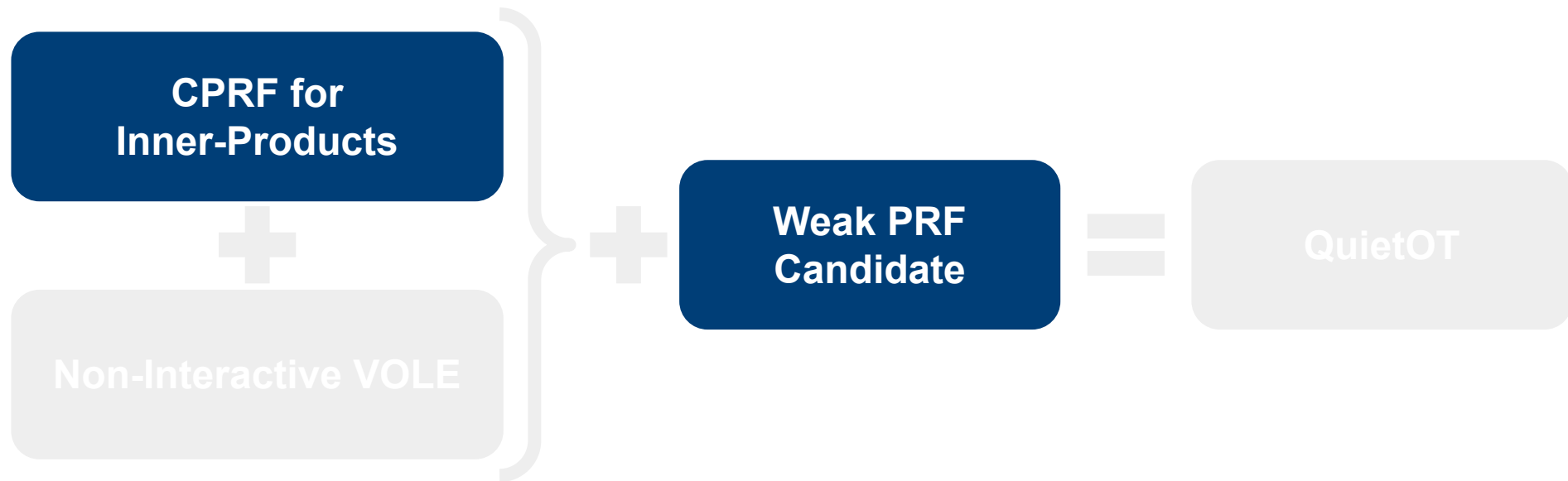
BIPSW weak PRF candidate: [BIPSW'18]

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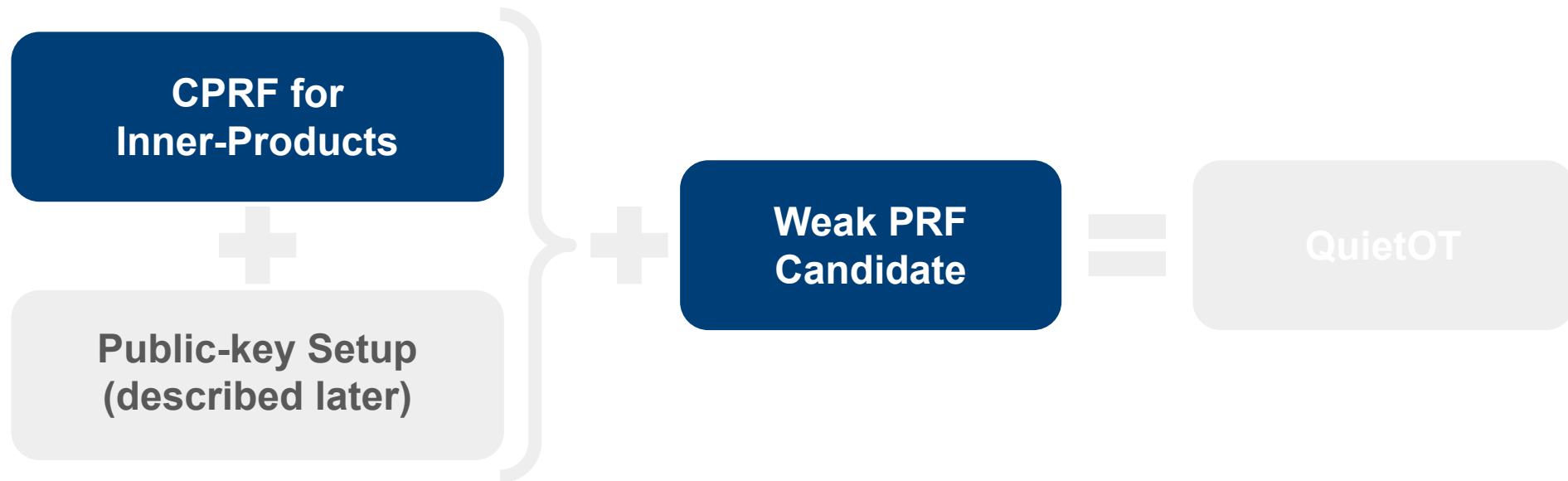
$$f_{\mathbf{k}}(\mathbf{x}) = 0 \iff \langle \mathbf{k}, \mathbf{x} \rangle \bmod 6 \in \{0, 1, 2\}$$

$$f_{\mathbf{k}}(\mathbf{x}) = 1 \iff \langle \mathbf{k}, \mathbf{x} \rangle \bmod 6 \in \{3, 4, 5\}$$

QuietOT: The main ingredients



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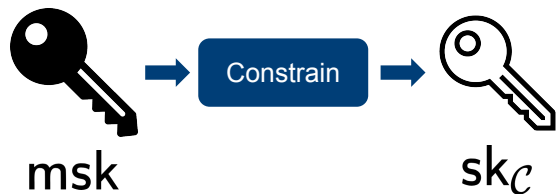


Putting things together

Idea: Use a PRF as the constraint predicate

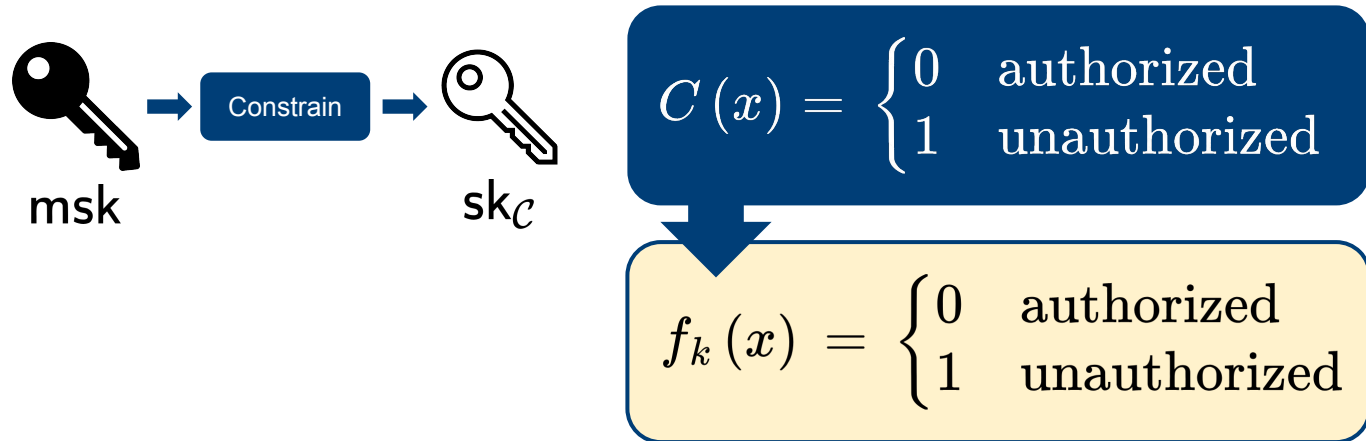
Inspired by previous constructions
building OT extension, in particular
[BCMPR'24]

Idea: Use a PRF as the constraint predicate

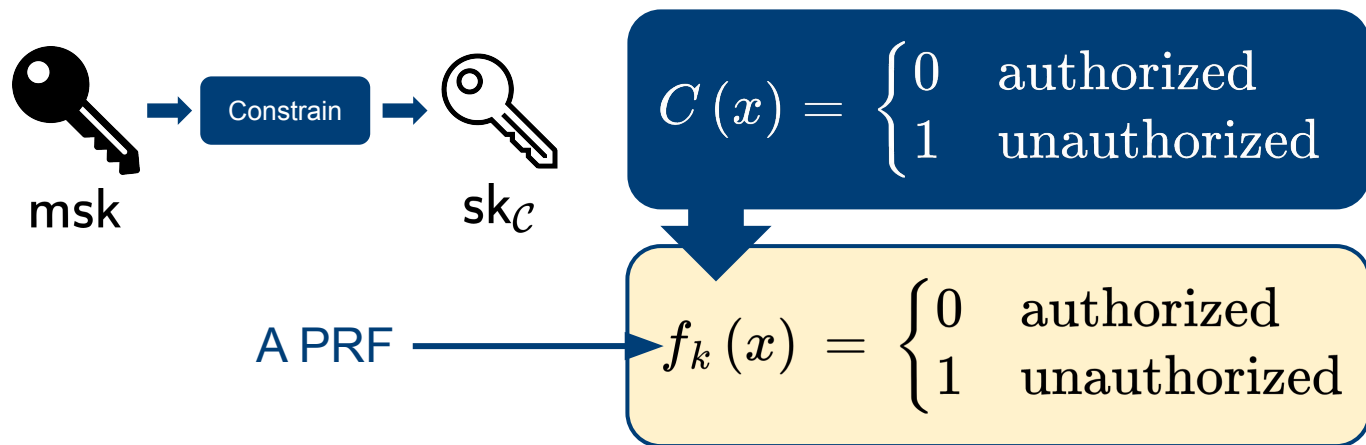


$$C(x) = \begin{cases} 0 & \text{authorized} \\ 1 & \text{unauthorized} \end{cases}$$

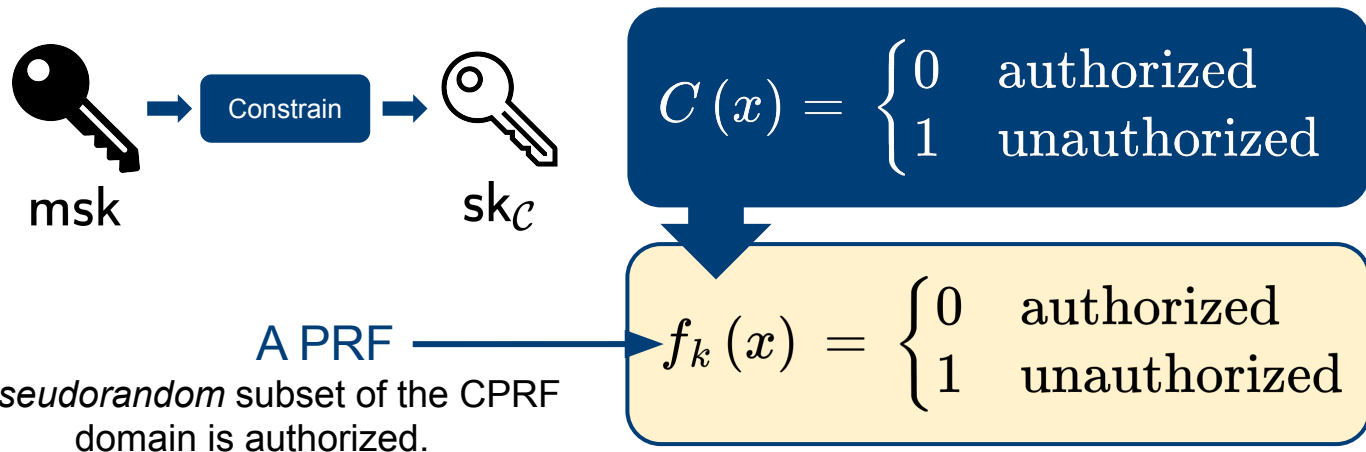
Idea: Use a PRF as the constraint predicate



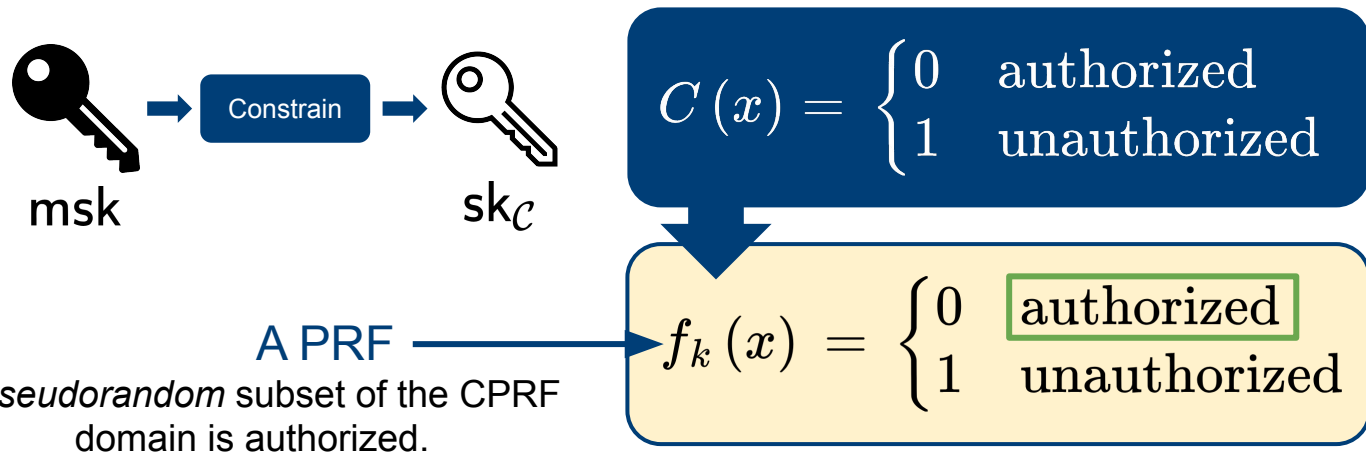
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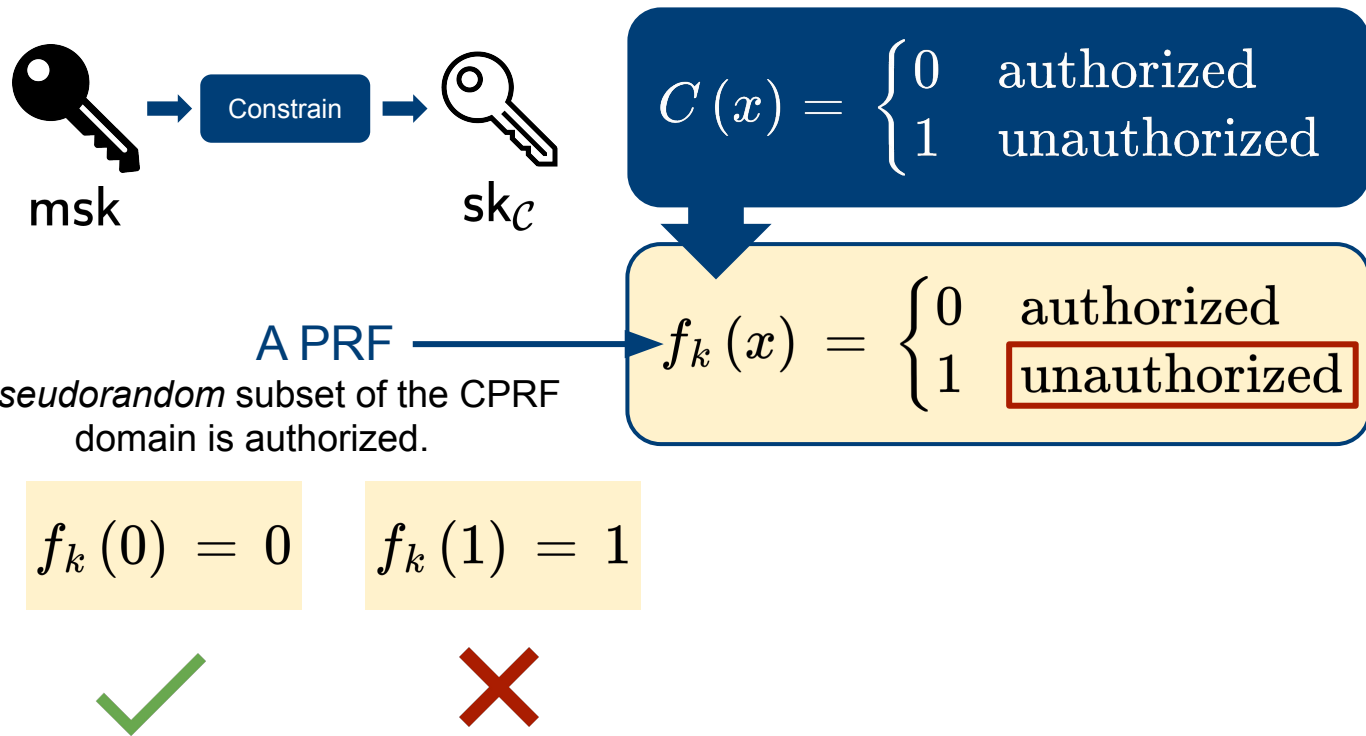
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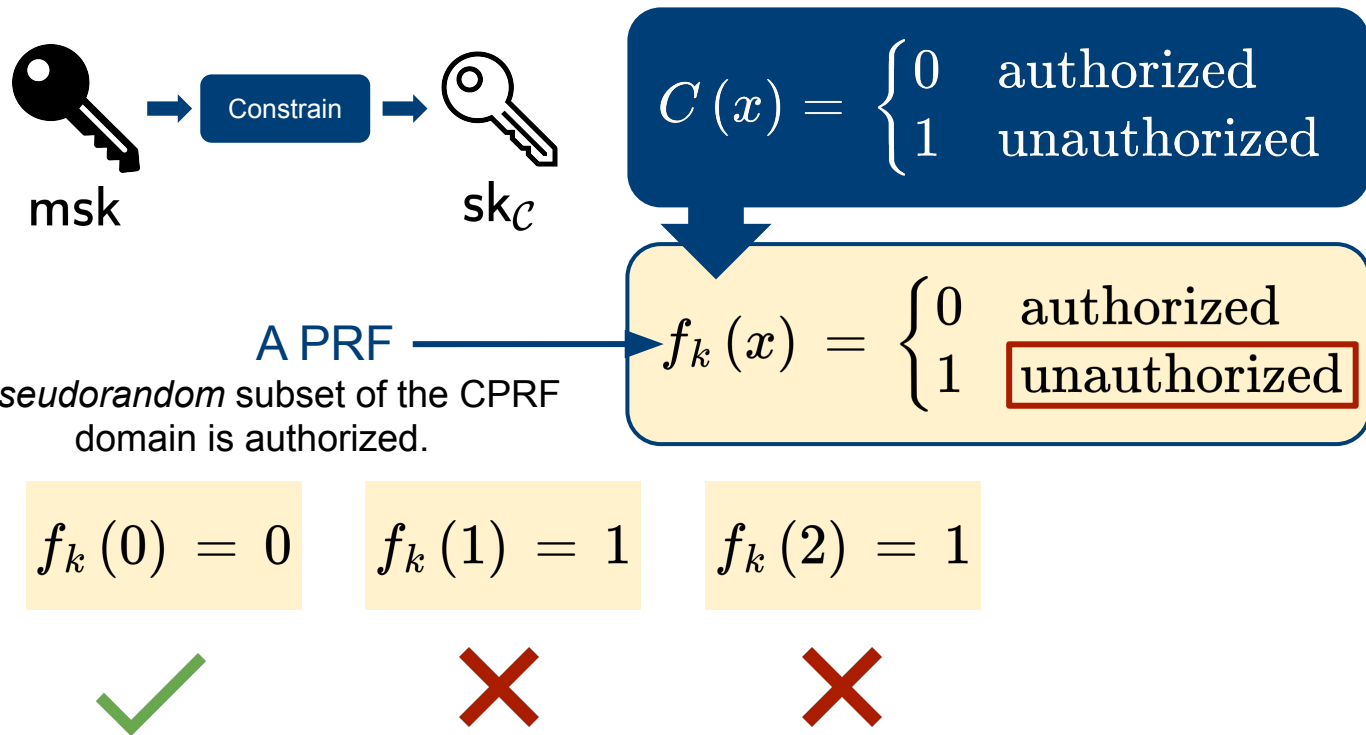
$$f_k(0) = 0$$



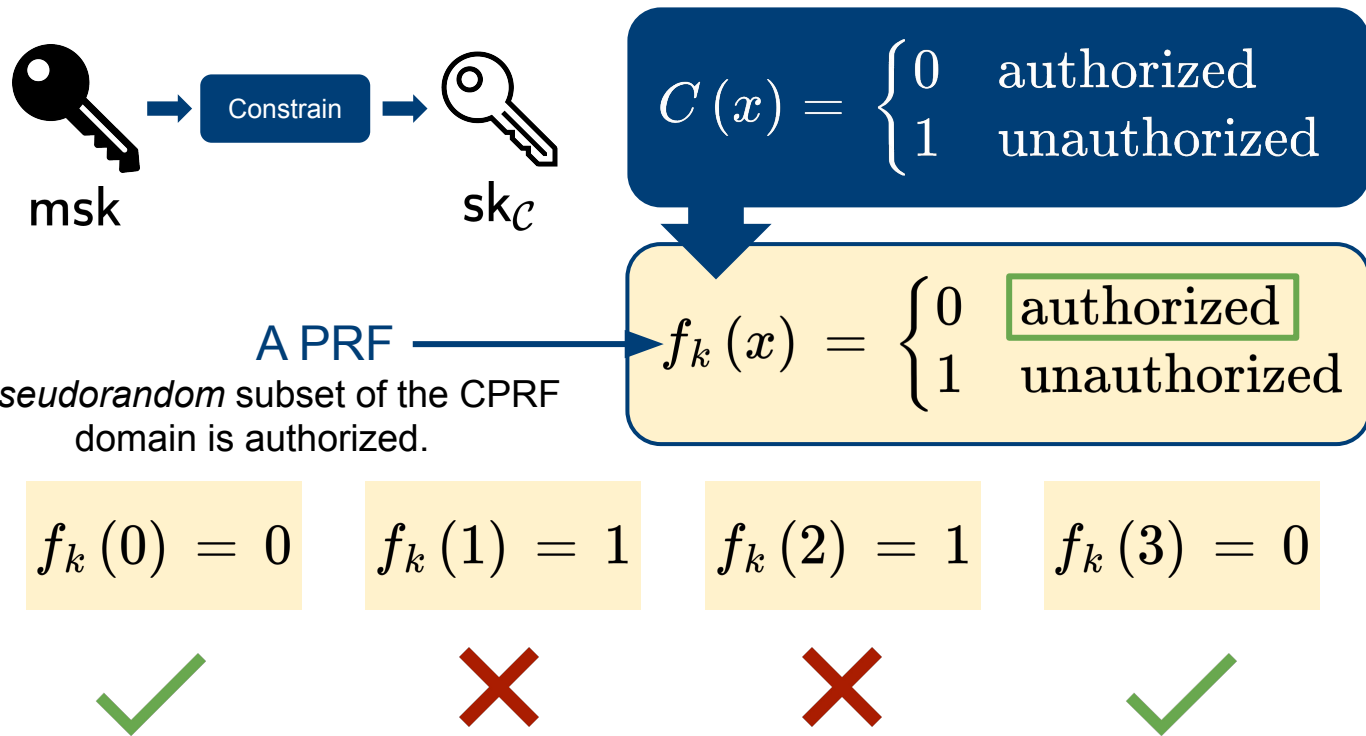
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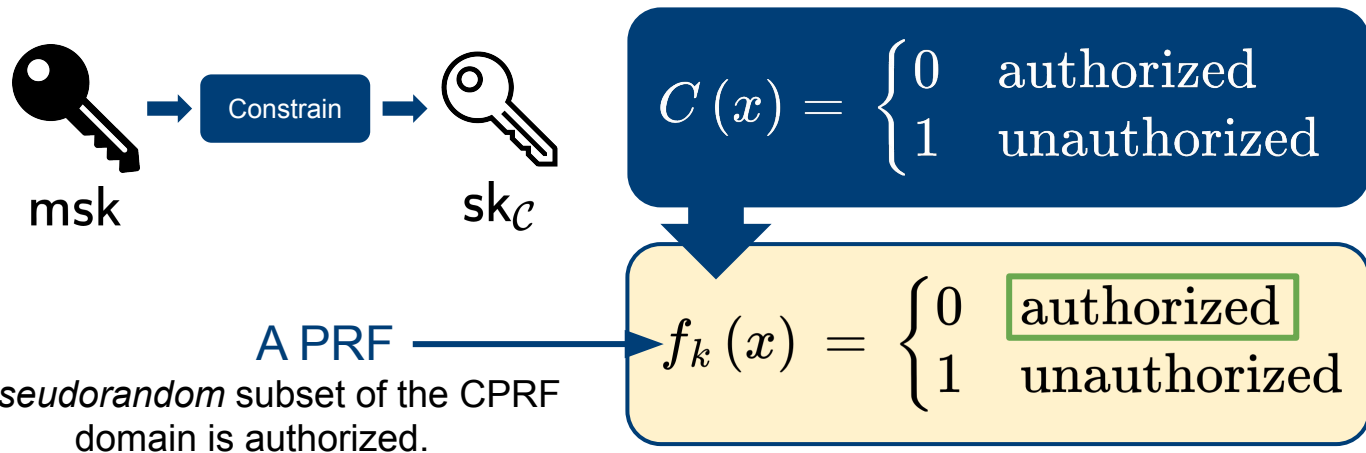
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Idea: Use a PRF as the constraint predicate



$$f_k(0) = 0$$



$$f_k(1) = 1$$



$$f_k(2) = 1$$



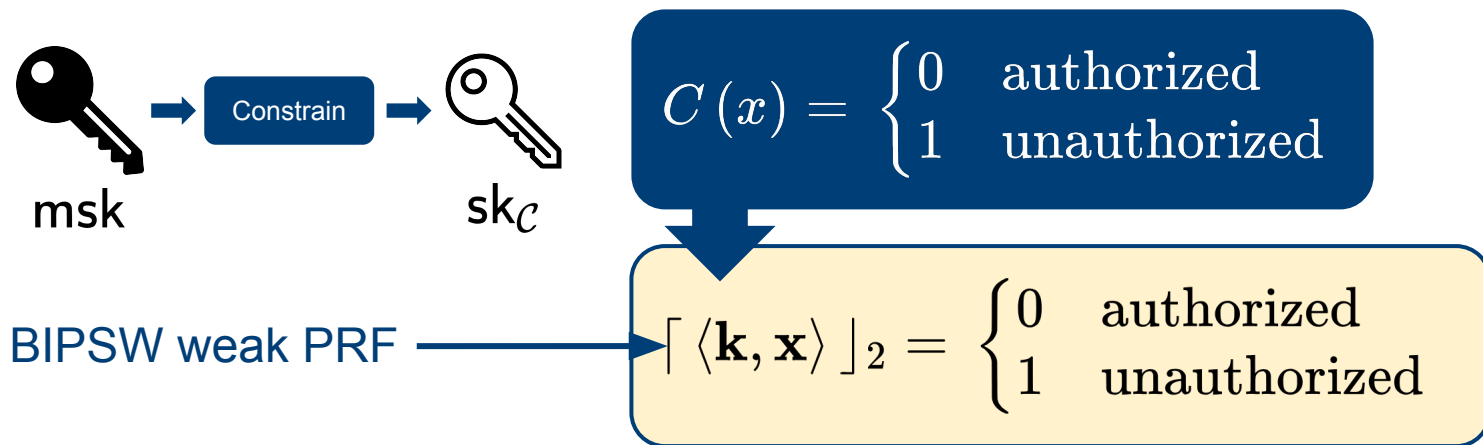
$$f_k(3) = 0$$



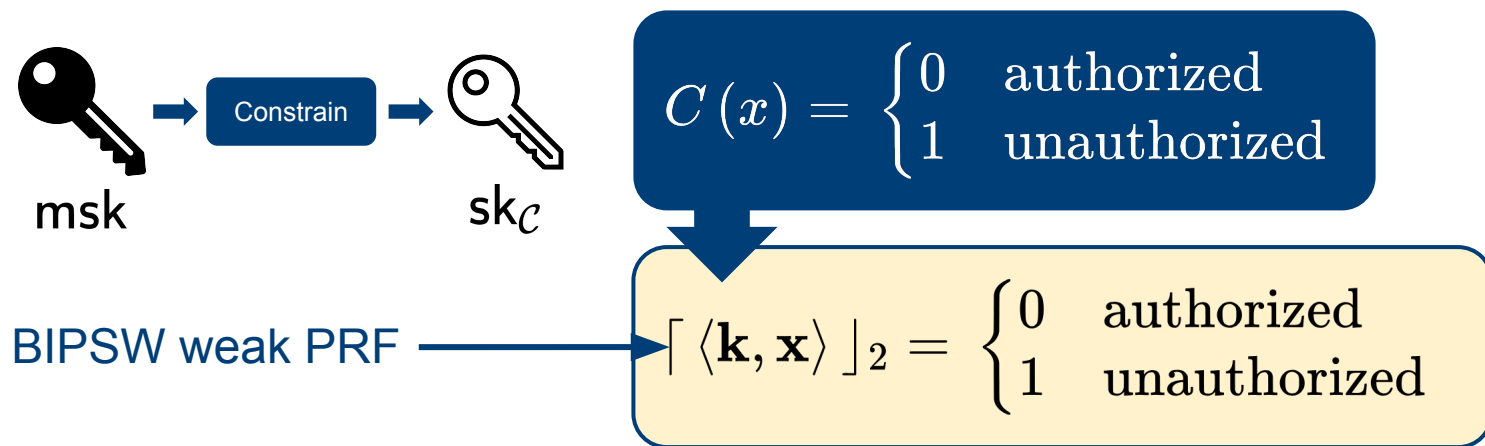
$$f_k(4) = 0$$



Idea: Use BIPSW weak PRF as the predicate

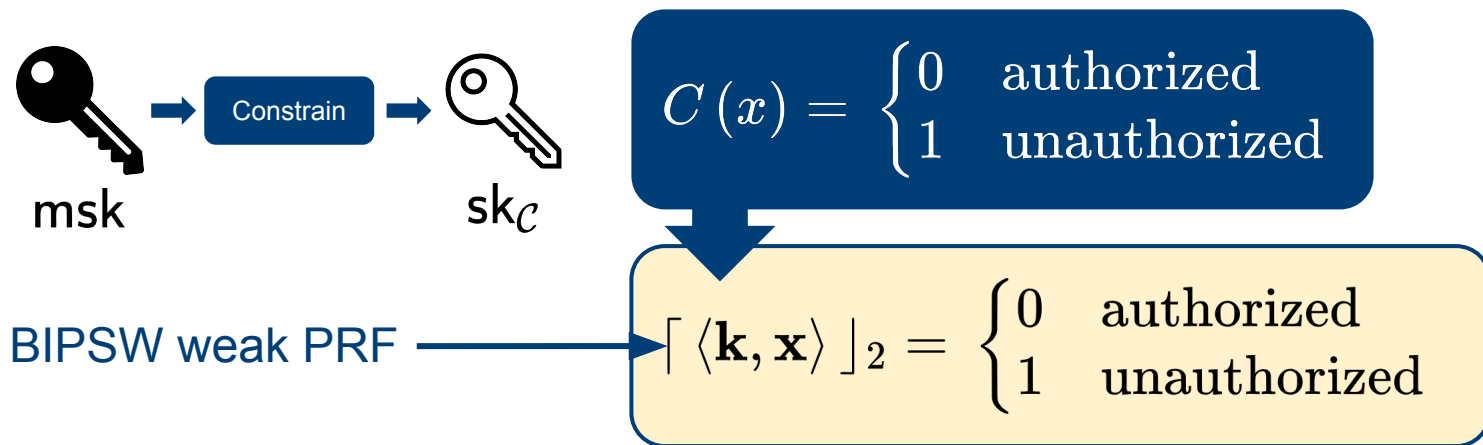


Idea: Use BIPSW weak PRF as the predicate



Problem: inner-product predicate isn't powerful enough

Idea: Use BIPSW weak PRF as the predicate



Solution: use many constrained PRFs!

OT Extension using CPRF + BIPSW weak PRF



Alice



Bob

OT Extension using CPRF + BIPSW weak PRF



Alice

Trusted Setup



Bob

OT Extension using CPRF + BIPSW weak PRF



Alice

Trusted Setup

$$\mathbf{k} \xleftarrow{R} \{0, 1\}^\lambda$$



Bob

OT Extension using CPRF + BIPSW weak PRF



Alice



msk_0

Trusted Setup

$$\mathbf{k} \xleftarrow{R} \{0, 1\}^\lambda$$

$$C_0(\mathbf{x}) = \langle \mathbf{k}, \mathbf{x} \rangle \bmod 6 - 0$$



sk_0

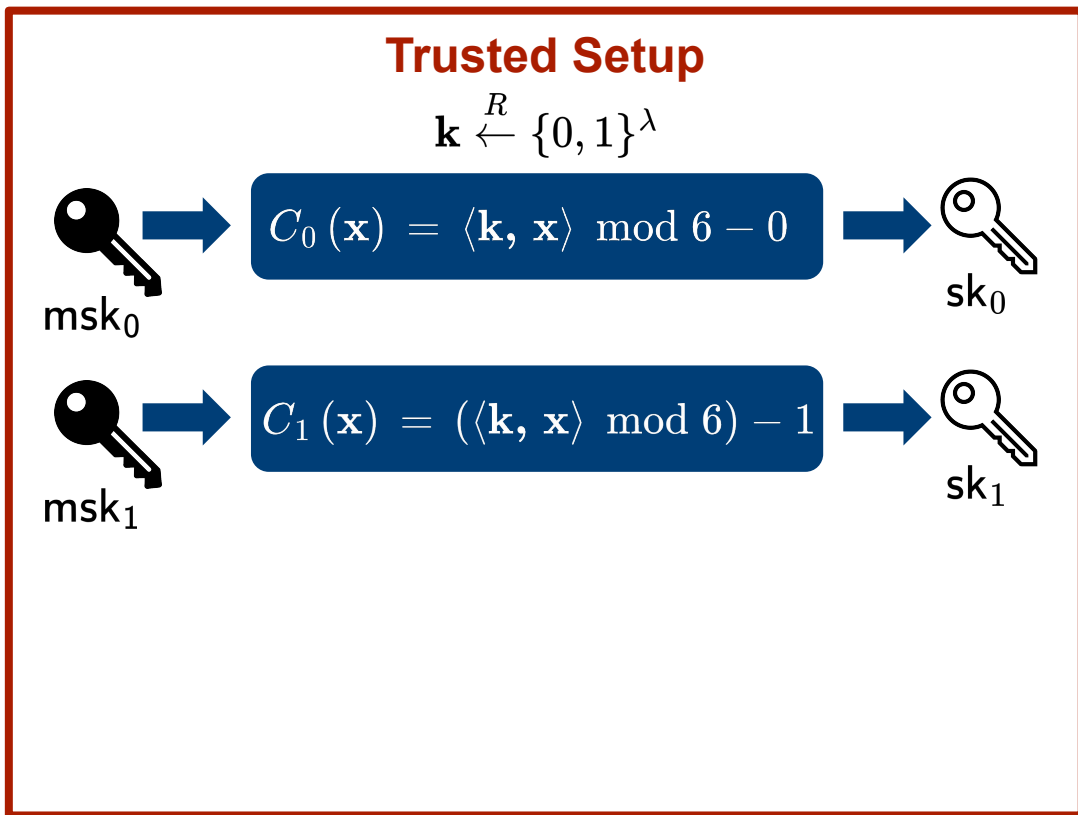


Bob

OT Extension using CPRF + BIPSW weak PRF



Alice

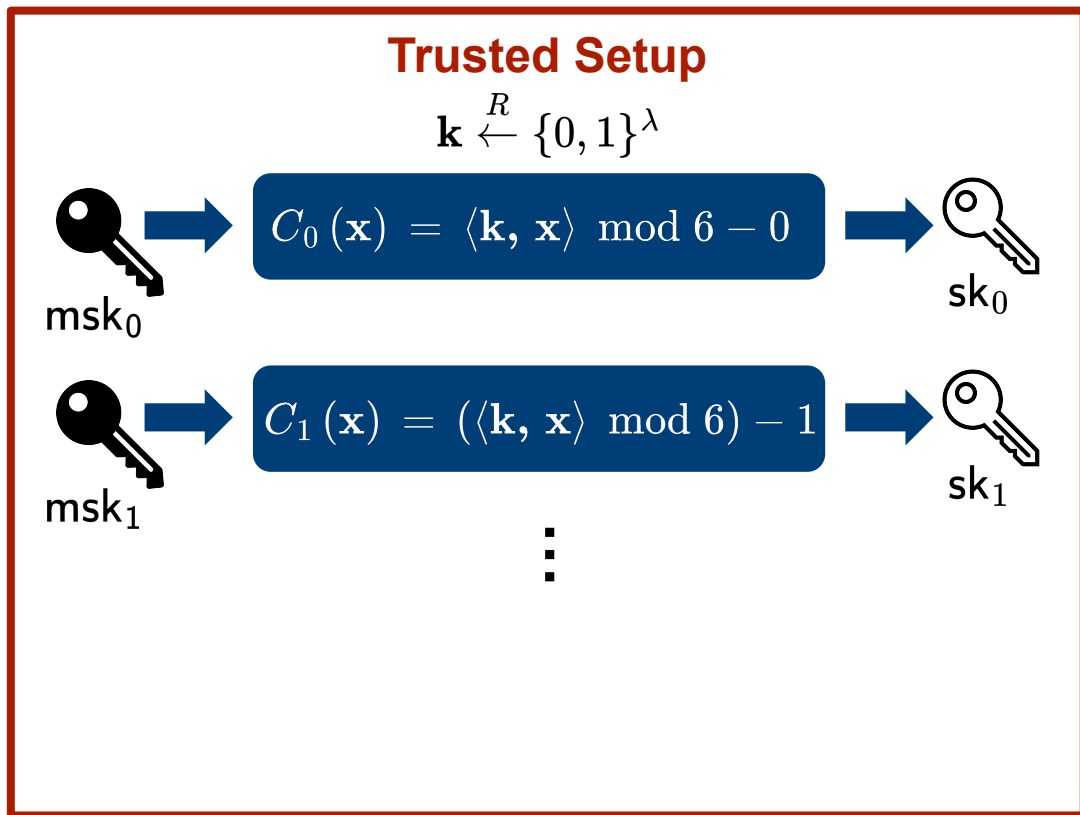


Bob

OT Extension using CPRF + BIPSW weak PRF



Alice

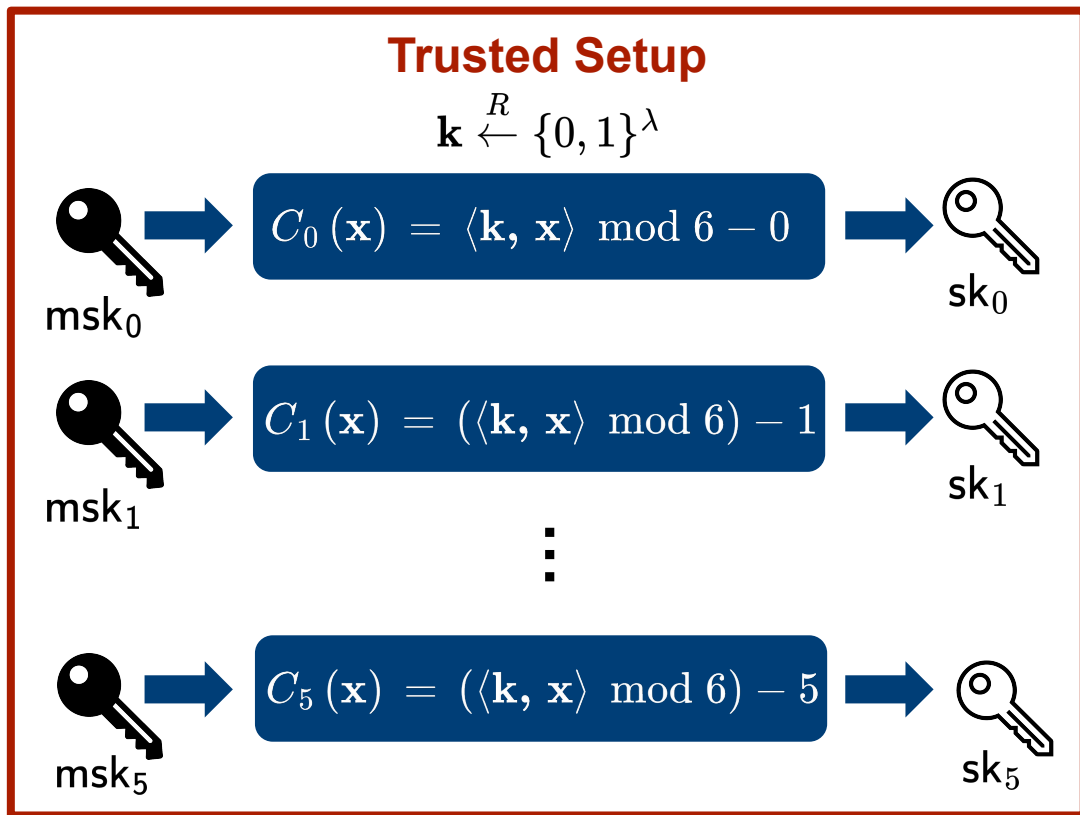


Bob

OT Extension using CPRF + BIPSW weak PRF

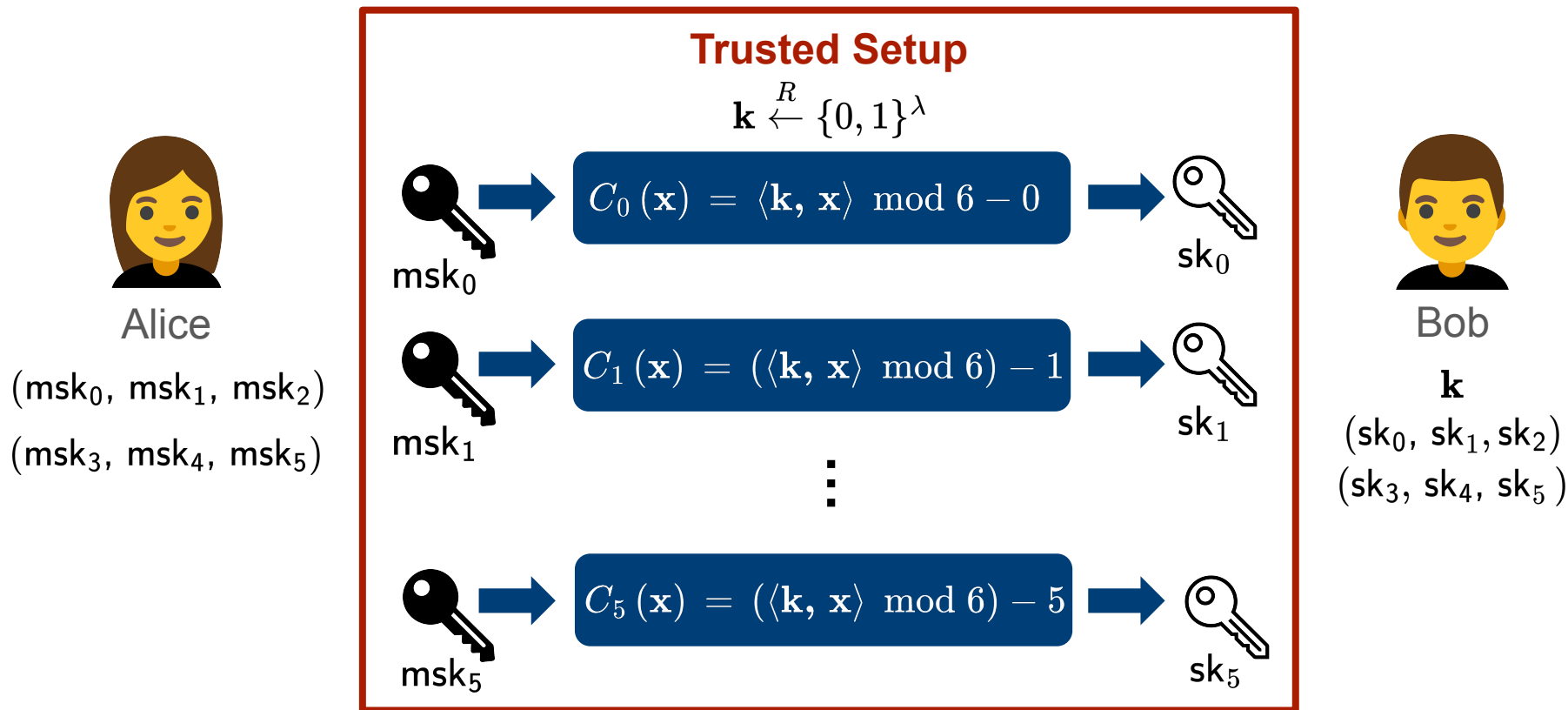


Alice



Bob

OT Extension using CPRF + BIPSW weak PRF



OT Extension using CPRF + BIPSW weak PRF



Alice

(msk_0, msk_1, msk_2)

(msk_3, msk_4, msk_5)



Bob

BIPSW weak PRF Key



k

(sk_0, sk_1, sk_2)

(sk_3, sk_4, sk_5)

OT Extension using CPRF + BIPSW weak PRF



Alice

(msk_0, msk_1, msk_2)

(msk_3, msk_4, msk_5)

**Constrained CPRF keys for each
possible inner product value
 $\{0,1,2,3,4,5\}$**



Bob

k

(sk_0, sk_1, sk_2)

(sk_3, sk_4, sk_5)

OT Extension using CPRF + BIPSW weak PRF



Alice

(msk_0, msk_1, msk_2)

(msk_3, msk_4, msk_5)



Master CPRF keys



Bob

k

(sk_0, sk_1, sk_2)

(sk_3, sk_4, sk_5)

OT Extension using CPRF + BIPSW weak PRF

For a public, random input \mathbf{X} :



Alice

$(\text{msk}_0, \text{msk}_1, \text{msk}_2)$

$(\text{msk}_3, \text{msk}_4, \text{msk}_5)$



Bob

\mathbf{k}

$(\text{sk}_0, \text{sk}_1, \text{sk}_2)$

$(\text{sk}_3, \text{sk}_4, \text{sk}_5)$

OT Extension using CPRF + BIPSW weak PRF

For a public, random input \mathbf{x} :



Alice

$(\text{msk}_0, \text{msk}_1, \text{msk}_2)$

$(\text{msk}_3, \text{msk}_4, \text{msk}_5)$

$$a_0 := \text{PRF}(\text{msk}_0, \mathbf{x})$$

$$a_1 := \text{PRF}(\text{msk}_1, \mathbf{x})$$

$$a_2 := \text{PRF}(\text{msk}_2, \mathbf{x})$$

$$a_3 := \text{PRF}(\text{msk}_3, \mathbf{x})$$

$$a_4 := \text{PRF}(\text{msk}_4, \mathbf{x})$$

$$a_5 := \text{PRF}(\text{msk}_5, \mathbf{x})$$



Bob

\mathbf{k}

$(\text{sk}_0, \text{sk}_1, \text{sk}_2)$

$(\text{sk}_3, \text{sk}_4, \text{sk}_5)$

OT Extension using CPRF + BIPSW weak PRF

For a public, random input \mathbf{x} :



Alice

$(\text{msk}_0, \text{msk}_1, \text{msk}_2)$

$(\text{msk}_3, \text{msk}_4, \text{msk}_5)$

$$a_0 := \text{PRF}(\text{msk}_0, \mathbf{x})$$

$$a_1 := \text{PRF}(\text{msk}_1, \mathbf{x})$$

$$a_2 := \text{PRF}(\text{msk}_2, \mathbf{x})$$

$$a_3 := \text{PRF}(\text{msk}_3, \mathbf{x})$$

$$a_4 := \text{PRF}(\text{msk}_4, \mathbf{x})$$

$$a_5 := \text{PRF}(\text{msk}_5, \mathbf{x})$$

$$\langle \mathbf{k}, \mathbf{x} \rangle \bmod 6 = 4$$



Bob

\mathbf{k}

$(\text{sk}_0, \text{sk}_1, \text{sk}_2)$

$(\text{sk}_3, \text{sk}_4, \text{sk}_5)$

OT Extension using CPRF + BIPSW weak PRF

For a public, random input \mathbf{x} :



Alice

$(\text{msk}_0, \text{msk}_1, \text{msk}_2)$

$(\text{msk}_3, \text{msk}_4, \text{msk}_5)$

$$a_0 := \text{PRF}(\text{msk}_0, \mathbf{x})$$

$$a_1 := \text{PRF}(\text{msk}_1, \mathbf{x})$$

$$a_2 := \text{PRF}(\text{msk}_2, \mathbf{x})$$

$$a_3 := \text{PRF}(\text{msk}_3, \mathbf{x})$$

$$a_4 := \text{PRF}(\text{msk}_4, \mathbf{x})$$

$$a_5 := \text{PRF}(\text{msk}_5, \mathbf{x})$$

$$\langle \mathbf{k}, \mathbf{x} \rangle \bmod 6 = 4$$

$$a_4 := \text{PRF}(\text{sk}_4, \mathbf{x})$$



Bob

\mathbf{k}

$(\text{sk}_0, \text{sk}_1, \text{sk}_2)$

$(\text{sk}_3, \text{sk}_4, \text{sk}_5)$

OT Extension using CPRF + BIPSW weak PRF

For a public, random input \mathbf{x} :



Alice

$(\text{msk}_0, \text{msk}_1, \text{msk}_2)$

$(\text{msk}_3, \text{msk}_4, \text{msk}_5)$

$$a_0 := \text{PRF}(\text{msk}_0, \mathbf{x})$$

$$a_1 := \text{PRF}(\text{msk}_1, \mathbf{x})$$

$$a_2 := \text{PRF}(\text{msk}_2, \mathbf{x})$$

$$a_3 := \text{PRF}(\text{msk}_3, \mathbf{x})$$

$$a_4 := \text{PRF}(\text{msk}_4, \mathbf{x})$$

$$a_5 := \text{PRF}(\text{msk}_5, \mathbf{x})$$

$$\langle \mathbf{k}, \mathbf{x} \rangle \bmod 6 = 4$$

$$a_4 := \text{PRF}(\text{sk}_4, \mathbf{x})$$



Bob

\mathbf{k}

$(\text{sk}_0, \text{sk}_1, \text{sk}_2)$

$(\text{sk}_3, \text{sk}_4, \text{sk}_5)$

OT Extension using CPRF + BIPSW weak PRF

For a public, random input \mathbf{x} :



Alice

$(\text{msk}_0, \text{msk}_1, \text{msk}_2)$

$(\text{msk}_3, \text{msk}_4, \text{msk}_5)$

$$a_0 := \text{PRF}(\text{msk}_0, \mathbf{x})$$

$$a_1 := \text{PRF}(\text{msk}_1, \mathbf{x})$$

$$a_2 := \text{PRF}(\text{msk}_2, \mathbf{x})$$

$$a_3 := \text{PRF}(\text{msk}_3, \mathbf{x})$$

$$a_4 := \text{PRF}(\text{msk}_4, \mathbf{x})$$

$$a_5 := \text{PRF}(\text{msk}_5, \mathbf{x})$$

$$\langle \mathbf{k}, \mathbf{x} \rangle \bmod 6 = 1$$

$$a_1 := \text{PRF}(\text{sk}_1, \mathbf{x})$$



Bob

\mathbf{k}

$(\text{sk}_0, \text{sk}_1, \text{sk}_2)$

$(\text{sk}_3, \text{sk}_4, \text{sk}_5)$

OT Extension using CPRF + BIPSW weak PRF

For a public, random input \mathbf{x} :



Alice

$(\text{msk}_0, \text{msk}_1, \text{msk}_2)$

$(\text{msk}_3, \text{msk}_4, \text{msk}_5)$

$$a_0 := \text{PRF}(\text{msk}_0, \mathbf{x})$$

$$a_1 := \text{PRF}(\text{msk}_1, \mathbf{x})$$

$$a_2 := \text{PRF}(\text{msk}_2, \mathbf{x})$$

$$a_3 := \text{PRF}(\text{msk}_3, \mathbf{x})$$

$$a_4 := \text{PRF}(\text{msk}_4, \mathbf{x})$$

$$a_5 := \text{PRF}(\text{msk}_5, \mathbf{x})$$

$$\langle \mathbf{k}, \mathbf{x} \rangle \bmod 6 = 1$$

$$a_1 := \text{PRF}(\text{sk}_1, \mathbf{x})$$



Bob

\mathbf{k}

$(\text{sk}_0, \text{sk}_1, \text{sk}_2)$

$(\text{sk}_3, \text{sk}_4, \text{sk}_5)$

OT Extension using CPRF + BIPSW weak PRF

For a public, random input \mathbf{x} :



Alice

$(\text{msk}_0, \text{msk}_1, \text{msk}_2)$

$(\text{msk}_3, \text{msk}_4, \text{msk}_5)$

$$a_0 := \text{PRF}(\text{msk}_0, \mathbf{x})$$

$$a_1 := \text{PRF}(\text{msk}_1, \mathbf{x})$$

$$a_2 := \text{PRF}(\text{msk}_2, \mathbf{x})$$

$$a_3 := \text{PRF}(\text{msk}_3, \mathbf{x})$$

$$a_4 := \text{PRF}(\text{msk}_4, \mathbf{x})$$

$$a_5 := \text{PRF}(\text{msk}_5, \mathbf{x})$$

$$\langle \mathbf{k}, \mathbf{x} \rangle \bmod 6 = 2$$

$$a_2 := \text{PRF}(\text{sk}_2, \mathbf{x})$$



Bob

\mathbf{k}

$(\text{sk}_0, \text{sk}_1, \text{sk}_2)$

$(\text{sk}_3, \text{sk}_4, \text{sk}_5)$

OT Extension using CPRF + BIPSW weak PRF

For a public, random input \mathbf{x} :



Alice

$(\text{msk}_0, \text{msk}_1, \text{msk}_2)$

$(\text{msk}_3, \text{msk}_4, \text{msk}_5)$

$$a_0 := \text{PRF}(\text{msk}_0, \mathbf{x})$$

$$a_1 := \text{PRF}(\text{msk}_1, \mathbf{x})$$

$$a_2 := \text{PRF}(\text{msk}_2, \mathbf{x})$$

$$a_3 := \text{PRF}(\text{msk}_3, \mathbf{x})$$

$$a_4 := \text{PRF}(\text{msk}_4, \mathbf{x})$$

$$a_5 := \text{PRF}(\text{msk}_5, \mathbf{x})$$

$$\langle \mathbf{k}, \mathbf{x} \rangle \bmod 6 = 2$$

$$a_2 := \text{PRF}(\text{sk}_2, \mathbf{x})$$



Bob

\mathbf{k}

$(\text{sk}_0, \text{sk}_1, \text{sk}_2)$

$(\text{sk}_3, \text{sk}_4, \text{sk}_5)$

Random-bit OT

Random-bit OT

Theorem [Beaver'96]: If there exists a *random-bit* OT protocol with R rounds, then there exists a *chosen-bit* OT protocol with R rounds.

Getting random-bit OT

In random-bit OT, Bob does not get to set the “choice bit” b



Alice

(m_0, m_1)



Bob

Getting random-bit OT

In random-bit OT, Bob does not get to set the “choice bit” b



Alice

(m_0, m_1)



Bob

(a_0, a_1, a_2)
 (a_3, a_4, a_5)



Computed using the CPRFs



(c, a_c)

Getting random-bit OT

In random-bit OT, Bob does not get to set the “choice bit” b



Alice

(m_0, m_1)

(a_0, a_1, a_2)

(a_3, a_4, a_5)

$(a_0 \oplus m_0, a_1 \oplus m_0, a_2 \oplus m_0)$
 $(a_3 \oplus m_1, a_4 \oplus m_1, a_5 \oplus m_1)$



Bob

(c, a_c)

Getting random-bit OT

In random-bit OT, Bob does not get to set the “choice bit” b



Alice

$$\begin{aligned} & (a_0 \oplus m_0, a_1 \oplus m_0, a_2 \oplus m_0) \\ & (a_3 \oplus m_1, a_4 \oplus m_1, a_5 \oplus m_1) \end{aligned}$$



Bob

$$(m_0, m_1)$$

$$\begin{aligned} & (a_0, a_1, a_2) \\ & (a_3, a_4, a_5) \end{aligned}$$

$$(c, a_c)$$

$$m_b := (m_b \oplus a_c) \oplus a_c$$

Getting random-bit OT

In random-bit OT, Bob does not get to set the “choice bit” b



Alice

$$\begin{aligned} & (a_0 \oplus m_0, a_1 \oplus m_0, a_2 \oplus m_0) \\ & (a_3 \oplus m_1, a_4 \oplus m_1, a_5 \oplus m_1) \end{aligned}$$



Bob

$$(m_0, m_1)$$

$$\begin{aligned} & (a_0, a_1, a_2) \\ & (a_3, a_4, a_5) \end{aligned}$$

$$(2, a_2)$$

$$m_0 := (m_0 \oplus a_2) \oplus a_2$$

Getting random-bit OT

In random-bit OT, Bob does not get to set the “choice bit” b



Alice

$$\begin{aligned} &(a_0 \oplus m_0, a_1 \oplus m_0, a_2 \oplus m_0) \\ &(\boxed{a_3 \oplus m_1}, a_4 \oplus m_1, a_5 \oplus m_1) \end{aligned}$$



Bob

$$(m_0, m_1)$$

$$(a_0, a_1, a_2)$$

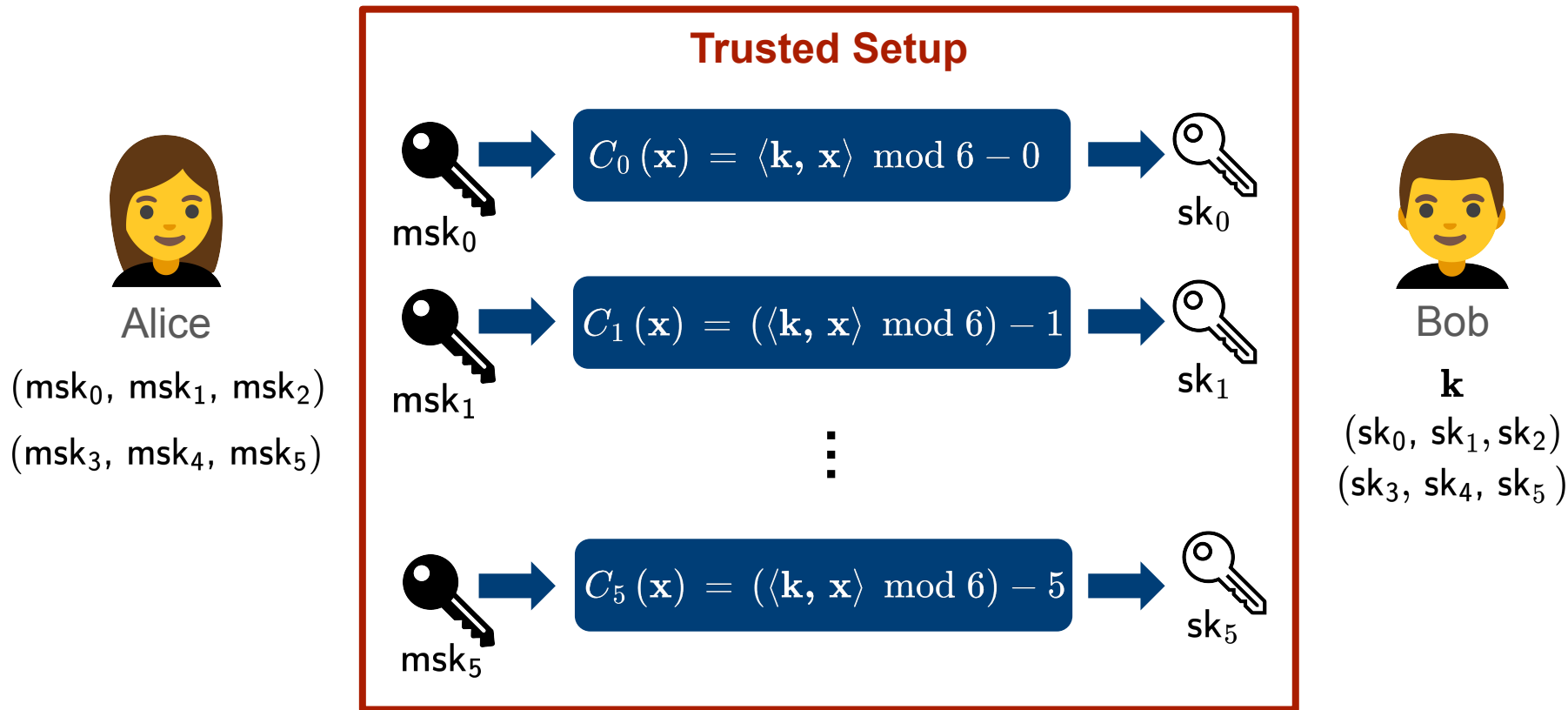
$$(a_3, a_4, a_5)$$

$$(3, a_3)$$

$$m_1 := (m_1 \oplus a_3) \oplus a_3$$

Public-key Setup

Obtaining a public-key setup



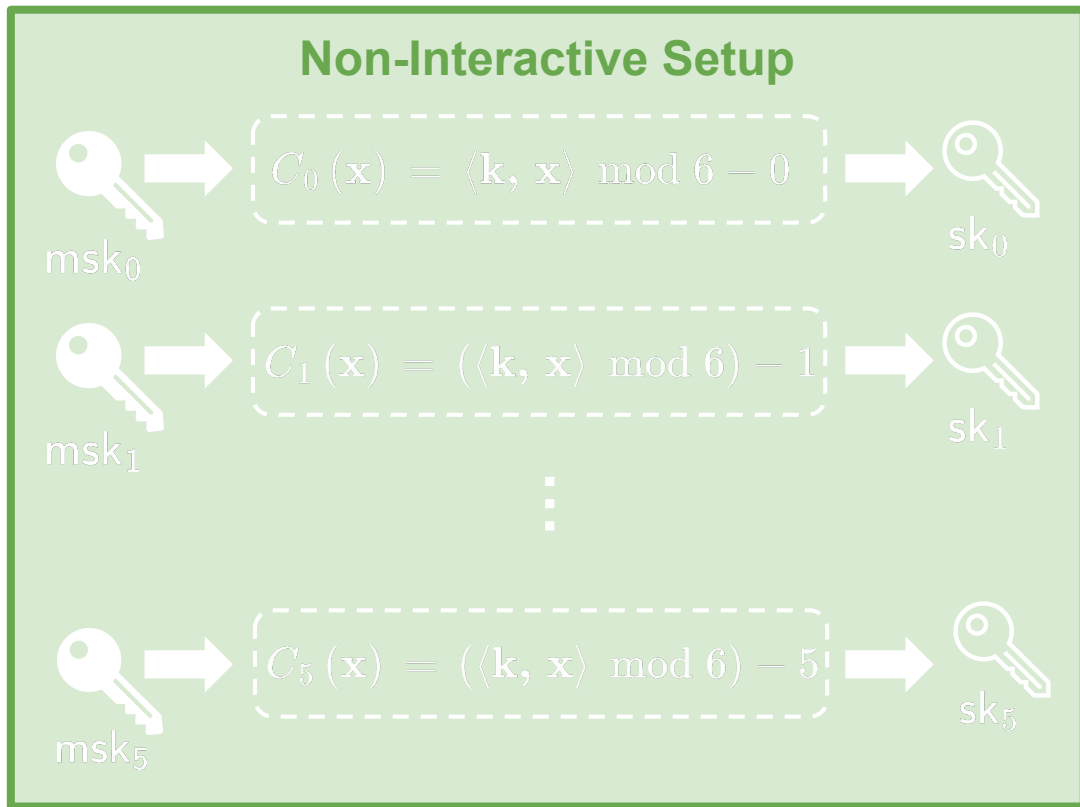
Obtaining a public-key setup



Alice

(msk_0, msk_1, msk_2)

(msk_3, msk_4, msk_5)



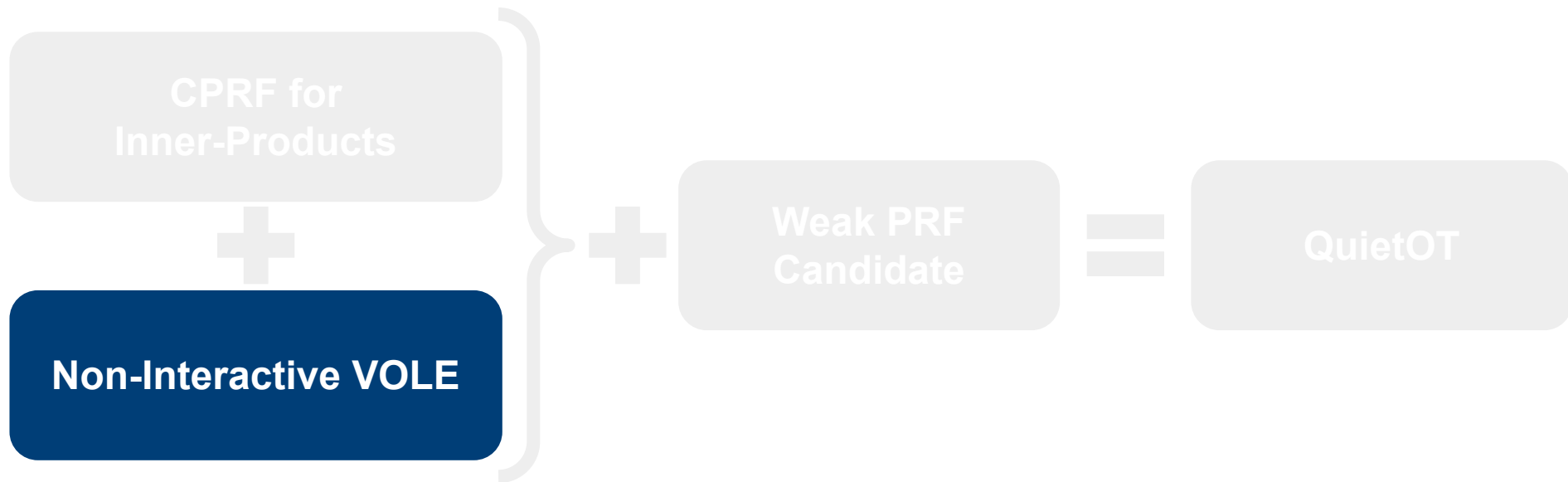
Bob

k

(sk_0, sk_1, sk_2)

(sk_3, sk_4, sk_5)

Obtaining a public-key setup



Obtaining a public-key setup

Constrained PRF for Inner-Product Predicates [S'24]

Let $H : \mathcal{R} \times \mathcal{R}^\ell \rightarrow \mathcal{Y}$ be a random oracle (RO).

Obtaining a public-key setup

Constrained PRF for Inner-Product Predicates [S'24]

Let $H : \mathcal{R} \times \mathcal{R}^\ell \rightarrow \mathcal{Y}$ be a random oracle (RO).

KeyGen(1^λ):

1. $\mathbf{z}_0 \xleftarrow{R} \mathcal{R}^\ell$
2. Return $\text{msk} := \mathbf{z}_0$

Constrain(msk, \mathbf{k}):

1. $\Delta \xleftarrow{R} \mathcal{R}$
2. $\mathbf{z}_1 := \mathbf{z}_0 - \Delta \mathbf{k}$
3. Return $\text{sk}_z := \mathbf{z}_1$

Eval(msk, \mathbf{x}):

1. $k := \langle \mathbf{z}_0, \mathbf{x} \rangle$
2. Return $H(k, \mathbf{x})$

CEval(sk_z, \mathbf{x}):

1. $k := \langle \mathbf{z}_1, \mathbf{x} \rangle$
2. Output $H(k, \mathbf{x})$

Obtaining a public-key setup

Constrained PRF for Inner-Product Predicates [S'24]

Let $H : \mathcal{R} \times \mathcal{R}^\ell \rightarrow \mathcal{Y}$ be a random oracle (RO).



Alice

$$\Delta \xleftarrow{R} \mathcal{R}$$

KeyGen(1^λ):

1. $\mathbf{z}_0 \xleftarrow{R} \mathcal{R}^\ell$
2. Return $\text{msk} := \mathbf{z}_0$

Constrain(msk, \mathbf{k}):

1. $\Delta \xleftarrow{R} \mathcal{R}$
2. $\mathbf{z}_1 := \mathbf{z}_0 - \Delta \mathbf{k}$
3. Return $\text{sk}_{\mathbf{z}} := \mathbf{z}_1$



Bob

$$\mathbf{k} \in \mathcal{R}^\ell$$

Obtaining a public-key setup

Constrained PRF for Inner-Product Predicates [S'24]

Let $H : \mathcal{R} \times \mathcal{R}^\ell \rightarrow \mathcal{Y}$ be a random oracle (RO).



Alice

KeyGen(1^λ):

1. $\mathbf{z}_0 \xleftarrow{R} \mathcal{R}^\ell$
2. Return $\text{msk} := \mathbf{z}_0$

Constrain(msk, \mathbf{k}):

1. $\Delta \xleftarrow{R} \mathcal{R}$
2. $\mathbf{z}_1 := \mathbf{z}_0 - \Delta \mathbf{k}$
3. Return $\text{sk}_{\mathbf{z}} := \mathbf{z}_1$



Bob

$$\Delta \xleftarrow{R} \mathcal{R}$$

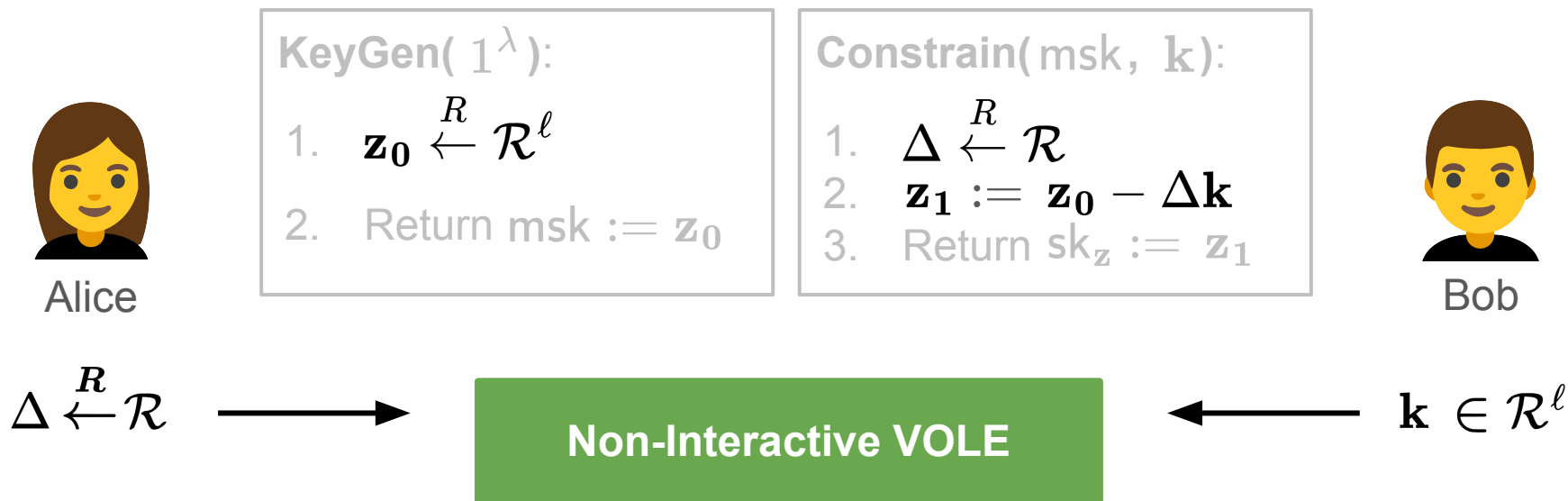
Non-Interactive VOLE

$$\mathbf{k} \in \mathcal{R}^\ell$$

Obtaining a public-key setup

Constrained PRF for Inner-Product Predicates [S'24]

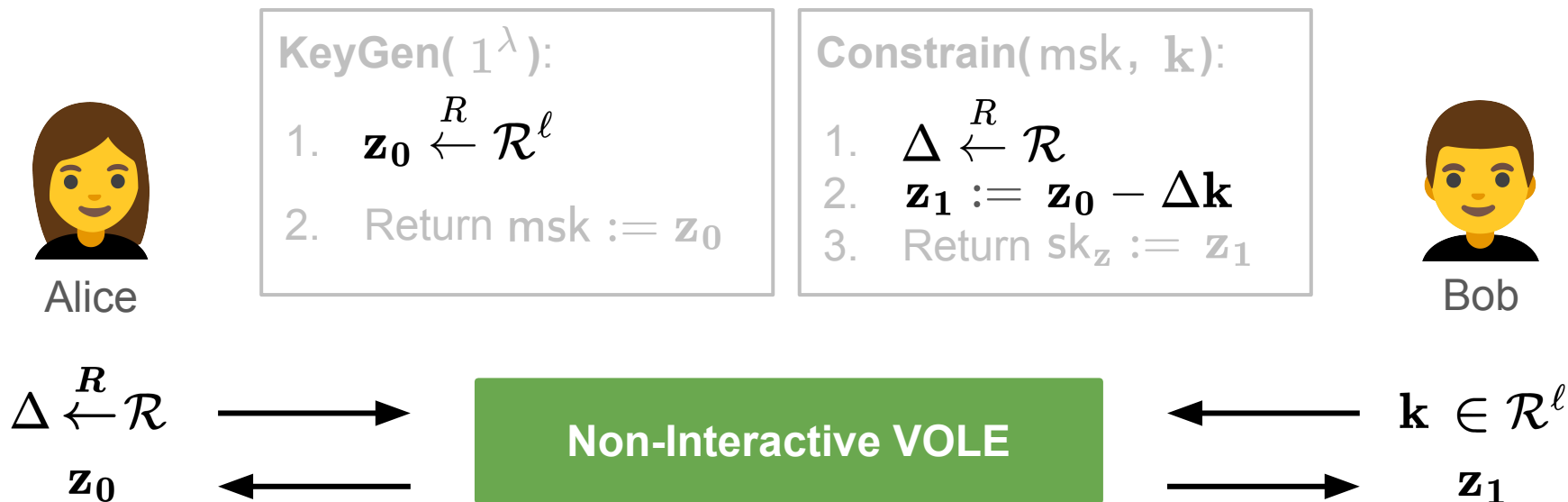
Let $H : \mathcal{R} \times \mathcal{R}^\ell \rightarrow \mathcal{Y}$ be a random oracle (RO).



Obtaining a public-key setup

Constrained PRF for Inner-Product Predicates [S'24]

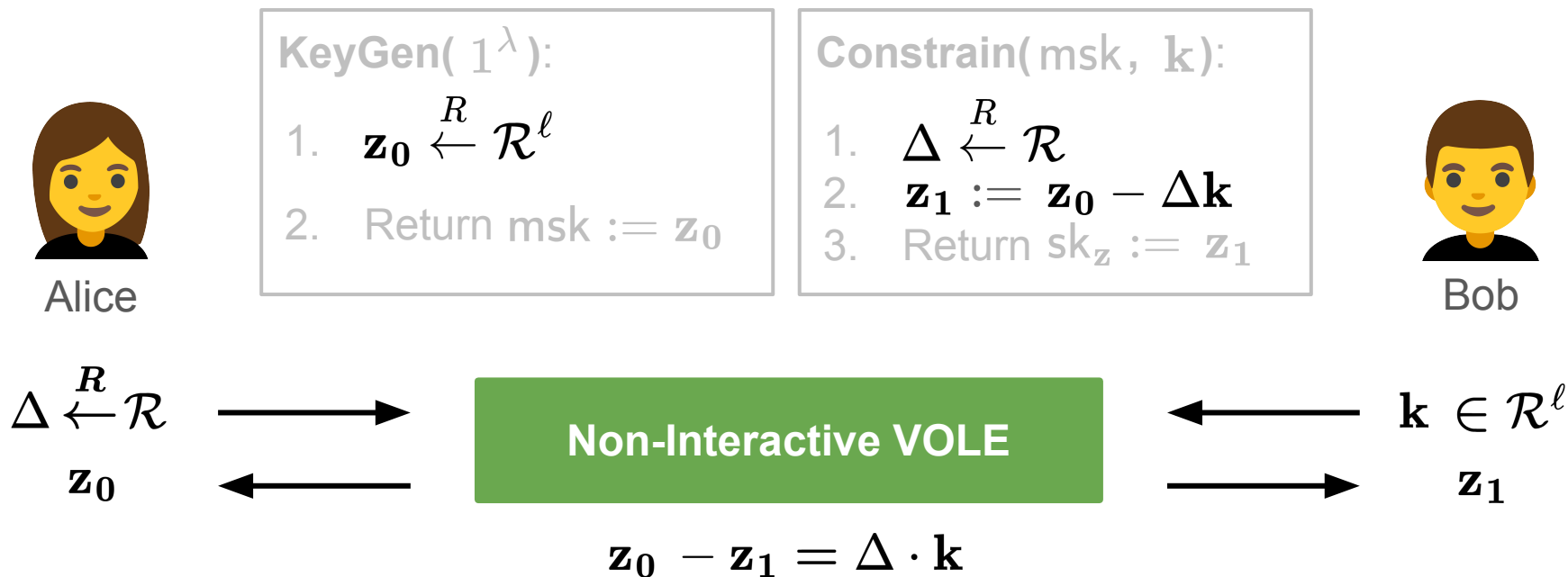
Let $H : \mathcal{R} \times \mathcal{R}^\ell \rightarrow \mathcal{Y}$ be a random oracle (RO).



Obtaining a public-key setup

Constrained PRF for Inner-Product Predicates [S'24]

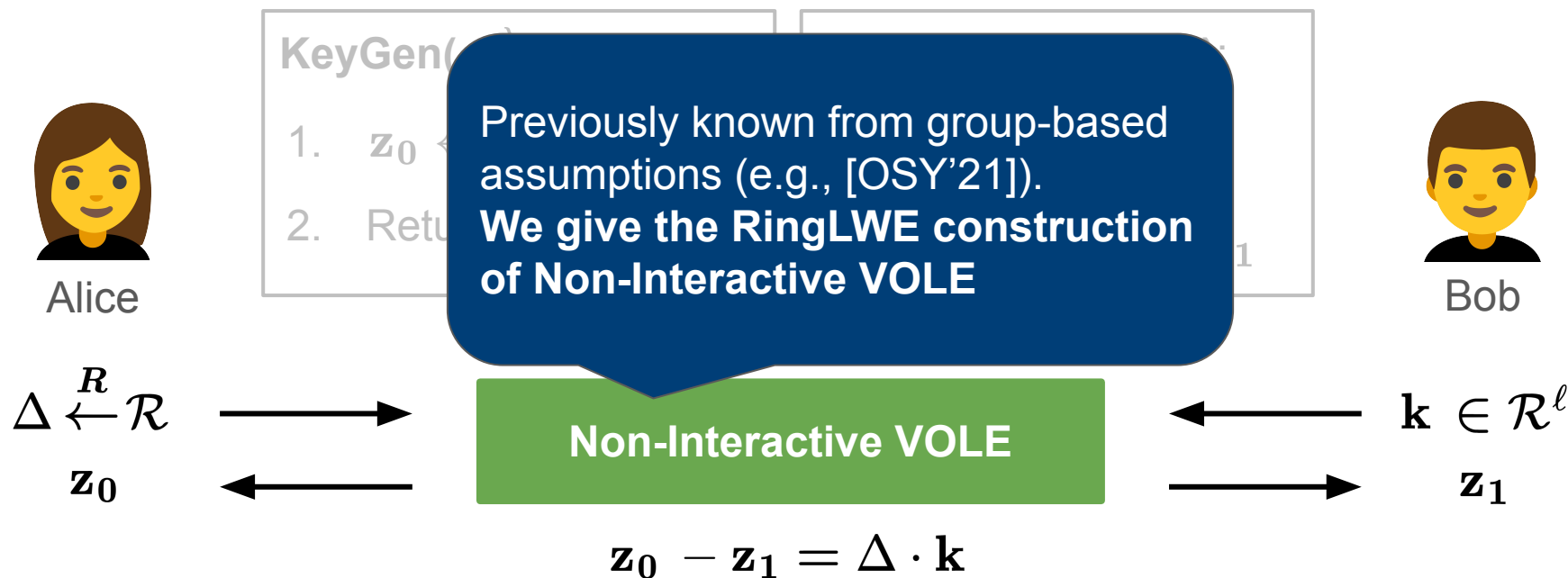
Let $H : \mathcal{R} \times \mathcal{R}^\ell \rightarrow \mathcal{Y}$ be a random oracle (RO).



Obtaining a public-key setup

Constrained PRF for Inner-Product Predicates [S'24]

Let $H : \mathcal{R} \times \mathcal{R}^\ell \rightarrow \mathcal{Y}$ be a random oracle (RO).



Implementation and Evaluation

Implementation and Evaluation

Artifact Badges: Available, Functional, and Reproduced.

<https://github.com/sachaservan/QuietOT>

Protocol	OT/s	Bits/OT
----------	------	---------

Protocol	OT/s	Bits/OT
SoftSpokenOT	44,443,000	32

Protocol	OT/s	Bits/OT
SoftSpokenOT	44,443,000	32
SoftSpokenOT	76,000	8

Protocol	OT/s	Bits/OT
SoftSpokenOT	44,443,000	32
SoftSpokenOT	76,000	8
RRT	6,856,000	3

Protocol	OT/s	Bits/OT
SoftSpokenOT	44,443,000	32
SoftSpokenOT	76,000	8
RRT	6,856,000	3
\mathbb{F}_4 OLEAGE	25,000,000	3

Protocol	OT/s	Bits/OT	Sender PK Size	Receiver PK Size
SoftSpokenOT	44,443,000	32	No Public Key Setup	
SoftSpokenOT	76,000	8		
RRT	6,856,000	3		
\mathbb{F}_4 OLEAGE	25,000,000	3		

Protocol	OT/s	Bits/OT	Sender PK Size	Receiver PK Size
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\mathbb{F}_4 OLEAGE	25,000,000	3		
OSY	1	3	50 KB	1 KB

Protocol	OT/s	Bits/OT	Sender PK Size	Receiver PK Size
SoftSpokenOT	44,443,000	32	No Public Key Setup	
SoftSpokenOT	76,000	8		
RRT	6,856,000	3		
\mathbb{F}_4 OLEAGE	25,000,000	3		
OSY	1	3	50 KB	1 KB
BCMPR	12,000	3	63 KB	72 KB

Protocol	OT/s	Bits/OT	Sender PK Size	Receiver PK Size
SoftSpokenOT	44,443,000	32	No Public Key Setup	
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BCMPR	12,000	3	63 KB	72 KB
QuietOT	561,000	7	5.4 MB	84 KB

Protocol	OT/s	Bits/OT	Sender PK Size	Receiver PK Size
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OSY	1	3	50 KB	1 KB
BCMPR	12,000	3	63 KB	72 KB
QuietOT	561,000	7	5.4 MB	84 KB
QuietOT (AVX3)	1,265,000	7	5.4 MB	84 KB

Protocol	OT/s	Bits/OT	Sender PK Size	Receiver PK Size
SoftSpokenOT	44,443,000	32	No Public Key Setup	
SoftSpokenOT	76,000	8		
RRT	6,856,000	3		
\mathbb{F}_4 OLEAGE	25,000,000	3		
OSY	1	3	For context, average website is 2MB in size	
BCMPR	12,000	3		
QuietOT	561,000	7	5.4 MB	84 KB
QuietOT (AVX3)	1,265,000	7	5.4 MB	84 KB

A lot more in the paper!

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- Another construction using a different weak PRF candidate

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- A “nearly-black-box” two-round OT extension in the ROM

A lot more in the paper!

- Another construction using a different weak PRF candidate
- A “nearly-black-box” two-round OT extension in the ROM
- A RingLWE-based Non-Interactive VOLE protocol

A lot more in the paper!

- Another construction using a different weak PRF candidate
- A “nearly-black-box” two-round OT extension in the ROM
- A RingLWE-based Non-Interactive VOLE protocol
- Pre-computability and other nice features

A lot more in the paper!

- Another construction using a different weak PRF candidate
- A “nearly-black-box” two-round OT extension in the ROM
- A RingLWE-based Non-Interactive VOLE protocol
- Pre-computability and other nice features

Open questions:

A lot more in the paper!

- Another construction using a different weak PRF candidate
- A “nearly-black-box” two-round OT extension in the ROM
- A RingLWE-based Non-Interactive VOLE protocol
- Pre-computability and other nice features

Open questions:

- Malicious security?

A lot more in the paper!

- Another construction using a different weak PRF candidate
- A “nearly-black-box” two-round OT extension in the ROM
- A RingLWE-based Non-Interactive VOLE protocol
- Pre-computability and other nice features

Open questions:

- Malicious security?
- Can we reach 50,000,000 OT/s with a public key setup?

Thank you!

Email: 3s@mit.edu

ePrint: ia.cr/2024/1079



QuietOT: Lightweight Oblivious Transfer with a Public-Key Setup

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Sacha Servan-Schreiber³

¹ CNRS

² IRIF, Université Paris Cité

³ MIT

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